
Techniques of Digital Holography For Microscopy and Metrology

International Workshop on Holographic Memories and Display
Nov. 15-16, 2010, University of Tokyo, Japn

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DHML: Digital Holography and Microscopy Laboratory

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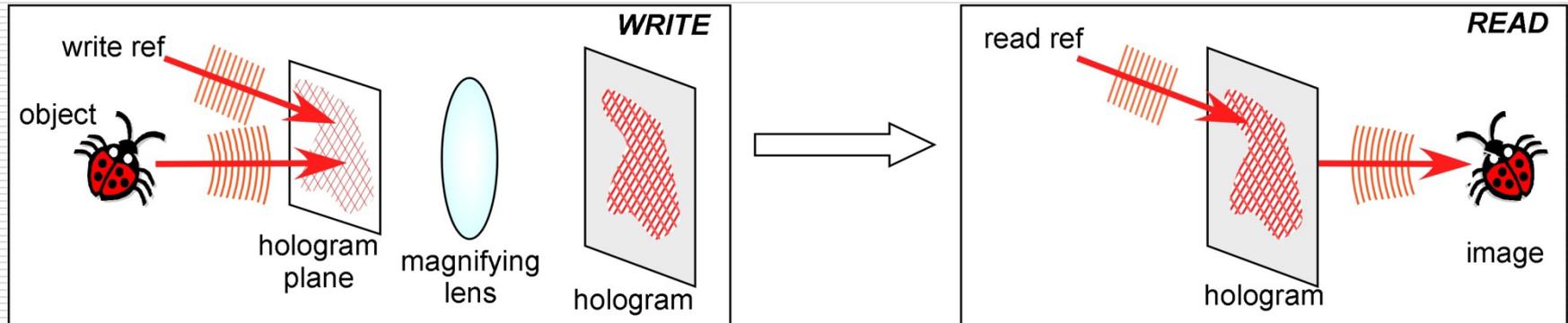
outline

- DHM: Digital Holographic Microscopy
- OPU: Optical Phase Unwrapping
- TIRHM: Total Internal Reflection Holographic Microscopy
- DHM of Laser Microsurgery
- Some current projects
- Optical Tomography and Topography
- Conclusions

outline

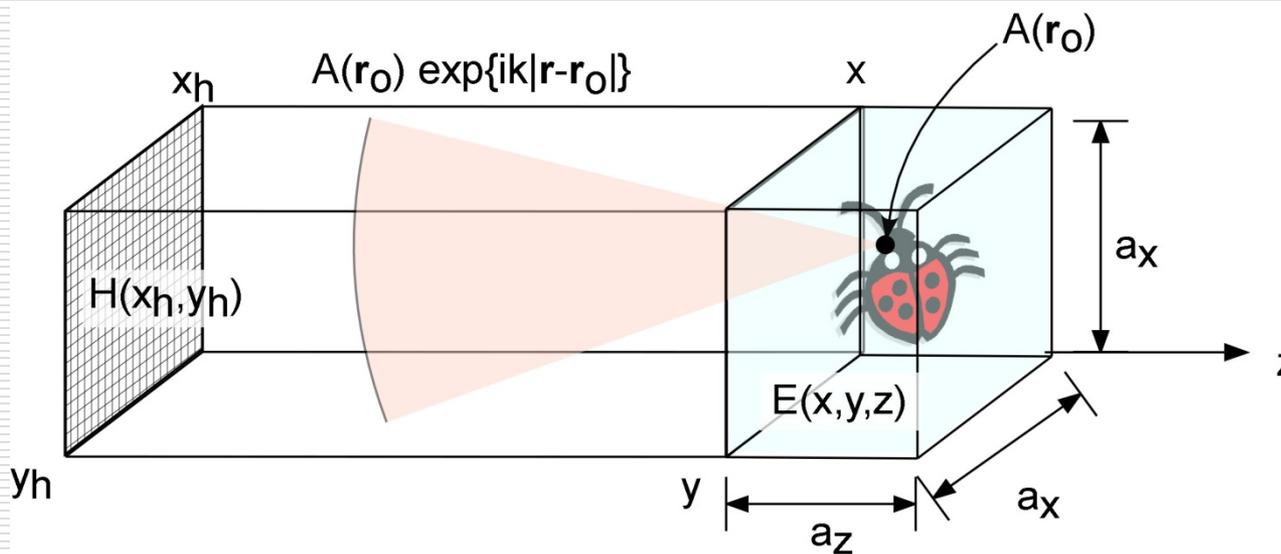
- ❑ **DHM: Digital Holographic Microscopy**
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Holography



- Generation of holographic interference by superposition of object and reference waves
- Reconstruction of holographic image by illumination of the hologram with another reference wave
- Real space holography: optical generation & optical reconstruction
- Computer generated holography (CGH): numerical generation & optical reconstruction
- Digital holography (DH): optical generation & numerical reconstruction

digital holography: general geometry



$$E(x, y) = -\frac{ik}{2\pi} \iint_{\Sigma} dx_0 dy_0 E_0(x_0, y_0) \frac{e^{ikr}}{r}$$

M. K. Kim, "Principles and techniques of digital holographic microscopy," SPIE Reviews 1, 50 (2010).

numerical diffraction : angular spectrum method

- Angular spectrum at $z = 0$

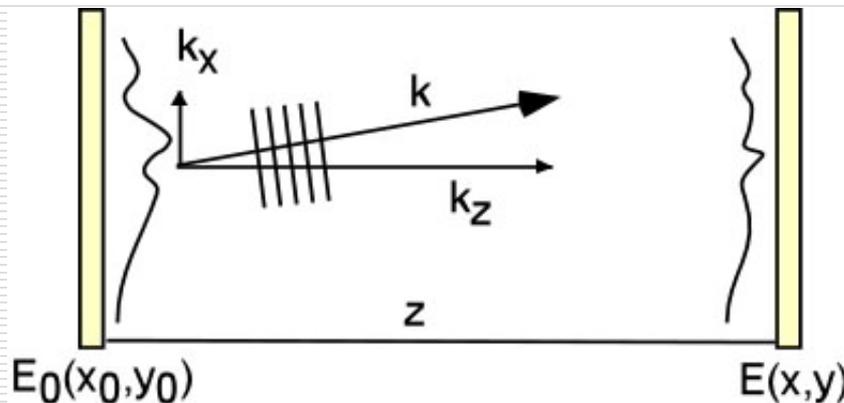
$$A(k_x, k_y; 0) = \mathcal{F} \{ E_0(x_0, y_0; 0) \} = \iint E_0(x_0, y_0; 0) \exp[-i(k_x x_0 + k_y y_0)] dx_0 dy_0$$

- Optical wave at $z = 0$

$$E_0(x_0, y_0; 0) = \mathcal{F}^{-1} \{ A(k_x, k_y; 0) \} = \iint A(k_x, k_y; 0) \exp[i(k_x x_0 + k_y y_0)] dk_x dk_y$$

- Optical field at z

$$\begin{aligned} E(x, y; z) &= \iint A(k_x, k_y; 0) \exp[ik_z z] \exp[i(k_x x + k_y y)] dk_x dk_y \\ &= \mathcal{F}^{-1} \{ \mathcal{F} \{ E_0 \} \exp[ik_z z] \} \end{aligned}$$

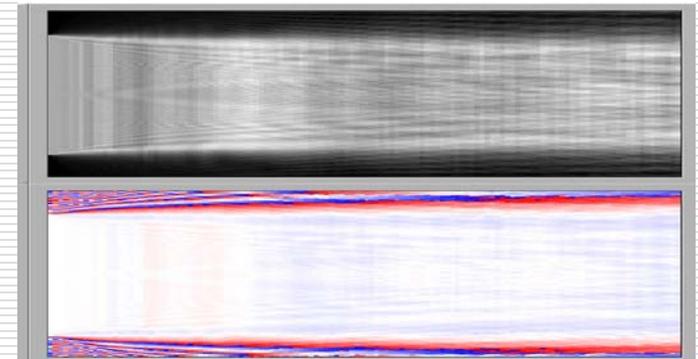
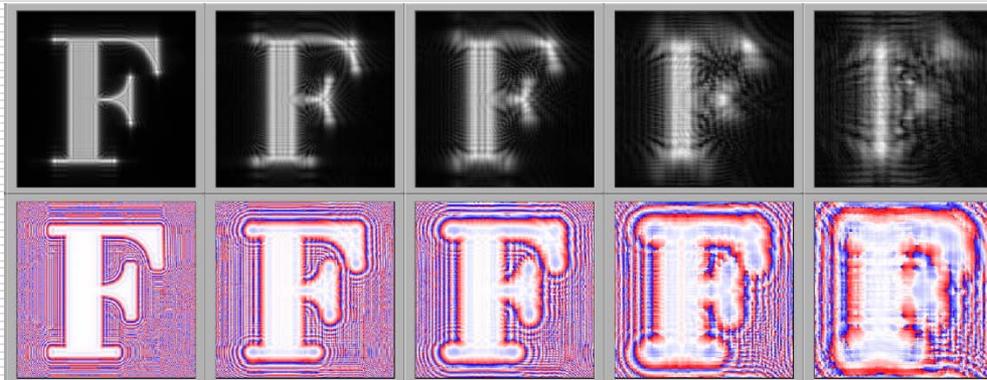


$$k_z = \sqrt{k^2 - k_x^2 - k_y^2}$$

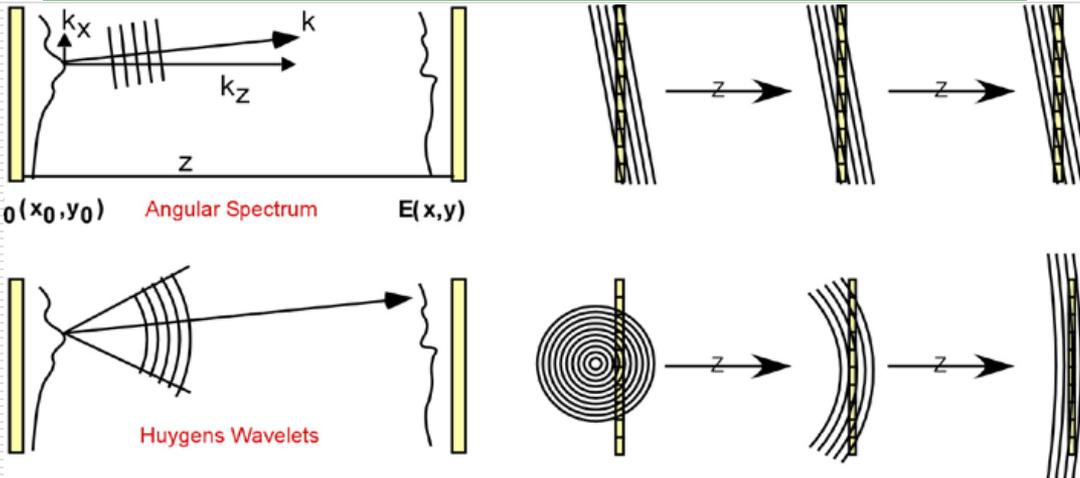
angular spectrum method

- plane wave decomposition
- two (2) Fourier transforms
 - one at $z = 0$, and
 - one at any arbitrary z
- no minimum distance requirement

- 3 peaks for off-axis holography
 - 0-order term: ref. and obj.
 - +/- 1st order: twin image terms
- numerical filtering of angular spectrum to suppress zero-order and twin image
 - noise control
- physical filtering by placing an aperture at a Fourier plane of hologram

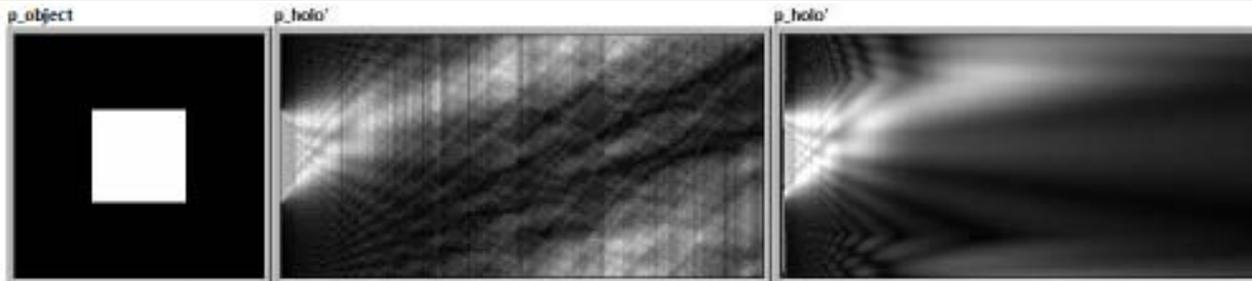


minimum & maximum distances



$$z_{\min} = X_0 \sqrt{\left(\frac{2\delta x}{\lambda}\right)^2 - 1}$$

$$z_{\max} = \frac{X_0^2}{2\lambda}$$



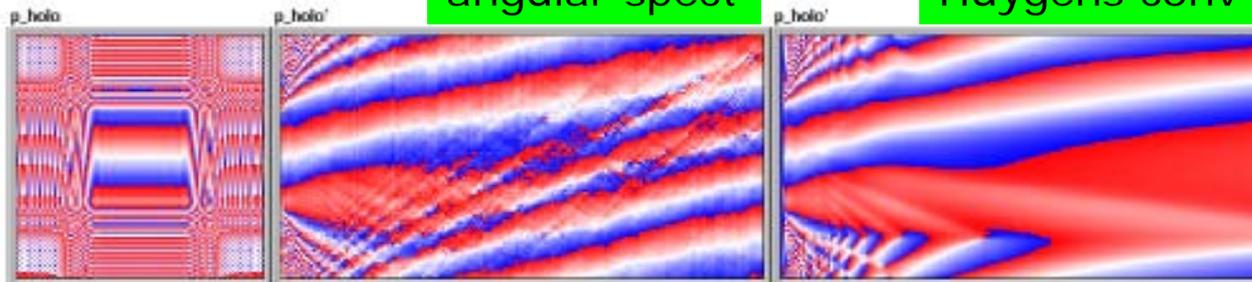
256 x 256 (256 x 256) 0.1

2E+4 x 256 (200 x 256)

2E+4 x 256 (200 x 256)

angular spect

Huygens conv



256 x 256 (256 x 256) 4.173E-7(1.368)

2E+4 x 256 (200 x 256) 8.142E-10(1.485)

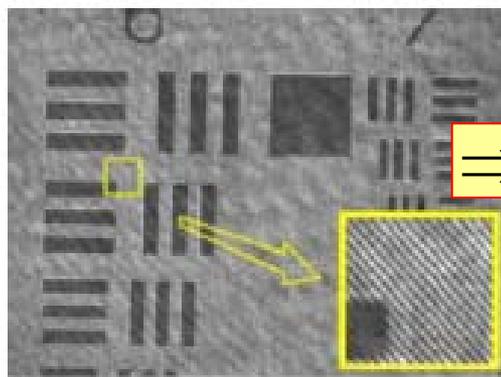
2E+4 x 256 (200 x 256) 1.179E-5(0.01062)

$z = 0 \sim 20,000 \mu\text{m}$

digital holography procedure

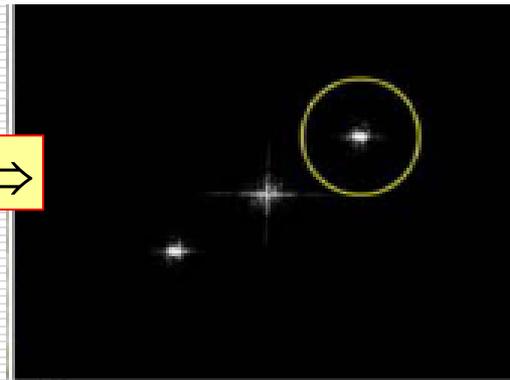
- HH': hologram
- FF: angular (Fourier) spectrum
- multiply propagation factor
- EEa: amplitude image
- EEp: phase image

$$E(x, y; z) = \mathcal{F}^{-1} \left\{ \mathcal{F} \{ E_0 \} \exp[ik_z z] \right\}$$



HH'

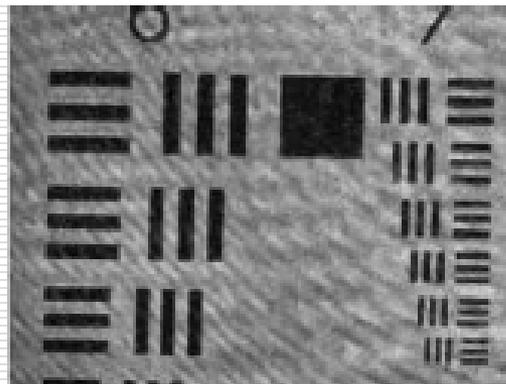
$\Rightarrow FFT \Rightarrow$



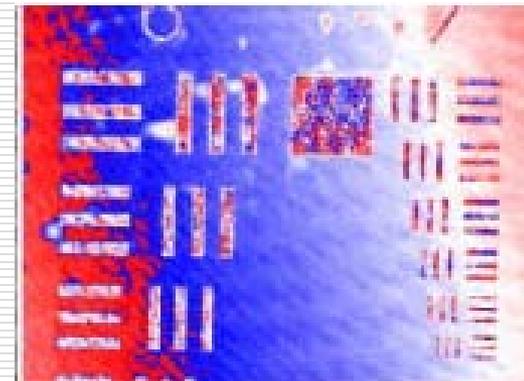
FF

$\times \exp(ik_z z)$

$\Rightarrow FFT^{-1} \Rightarrow$

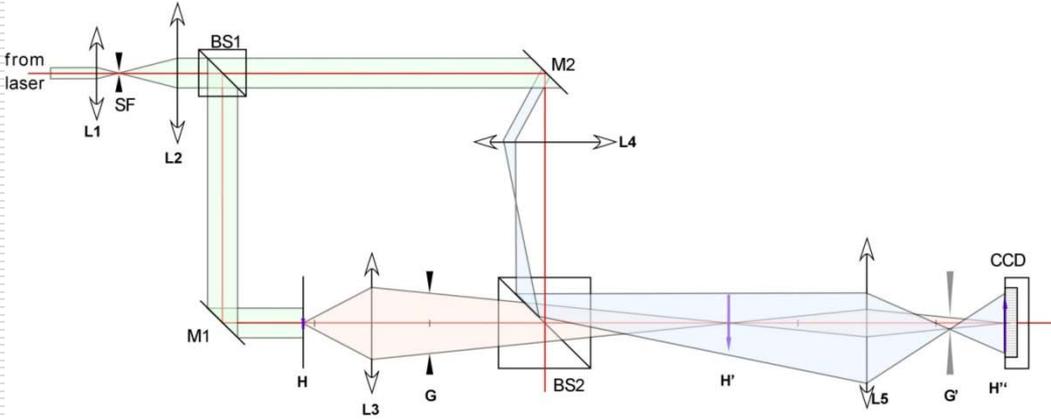
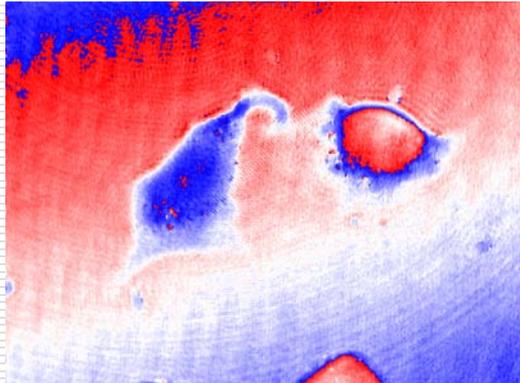
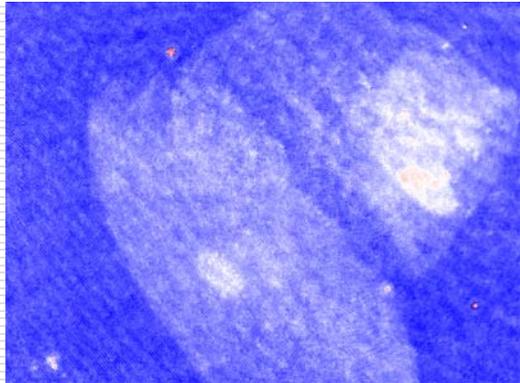
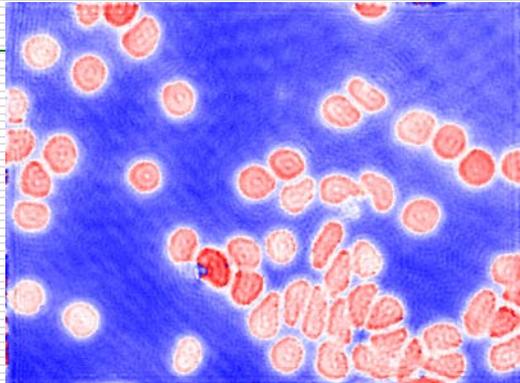
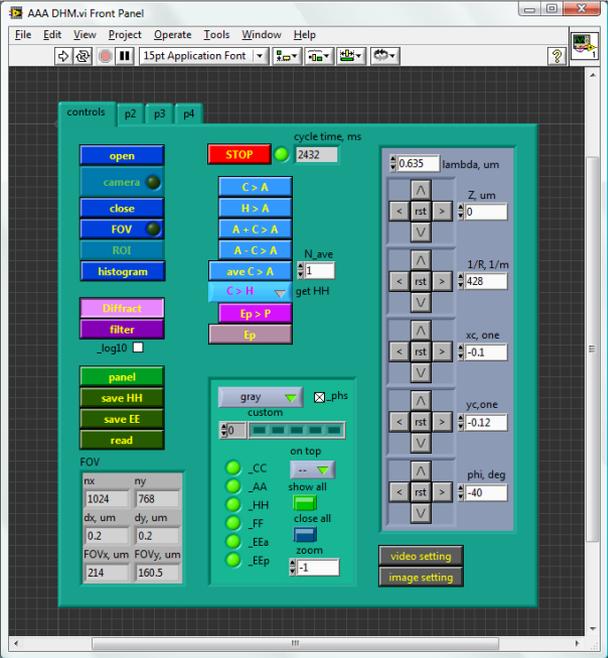
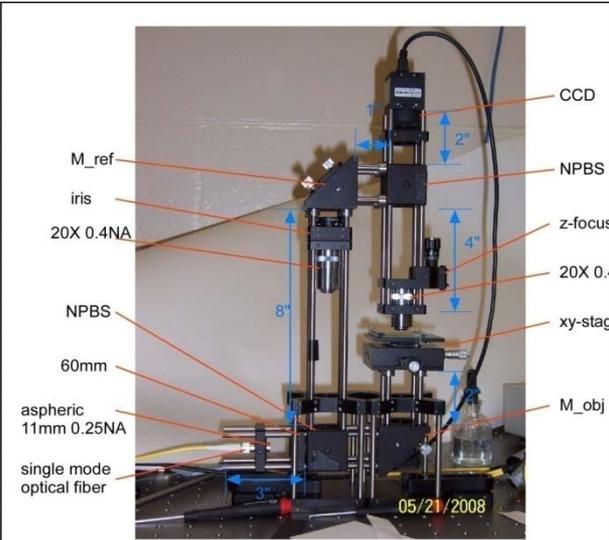


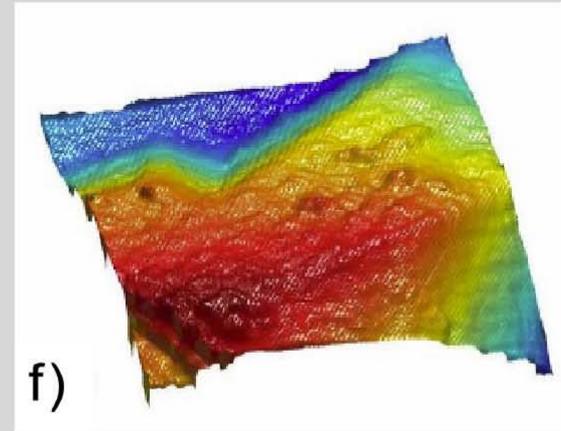
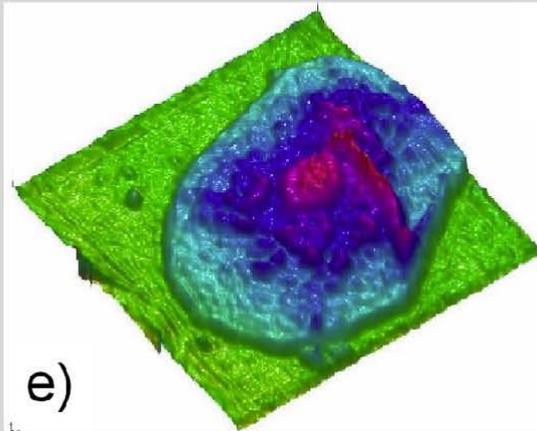
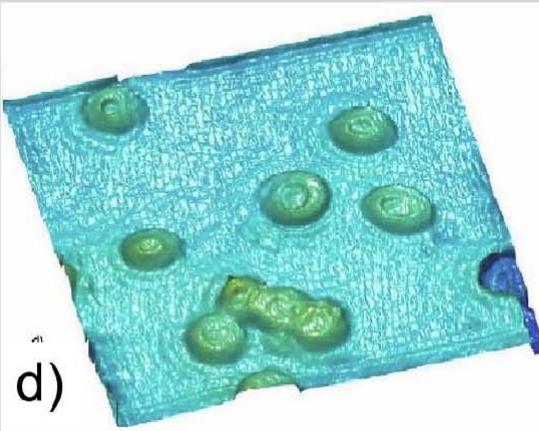
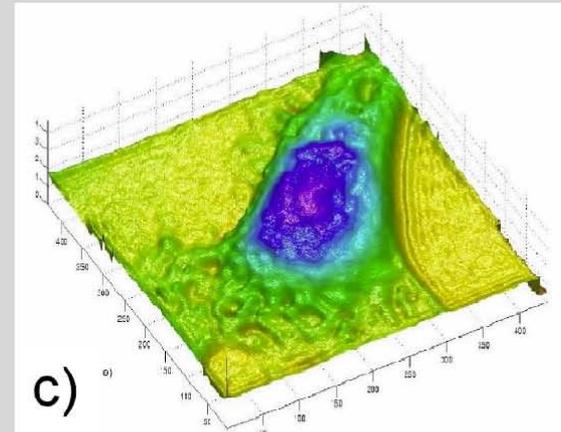
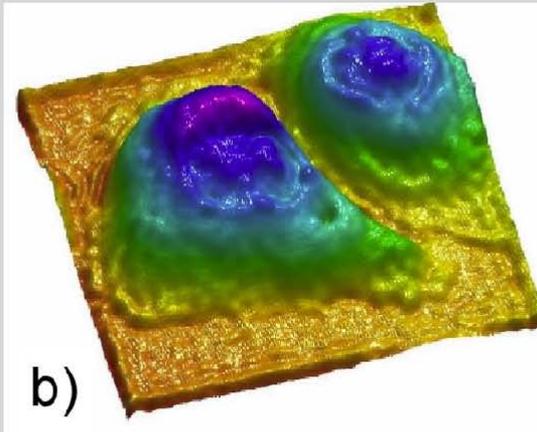
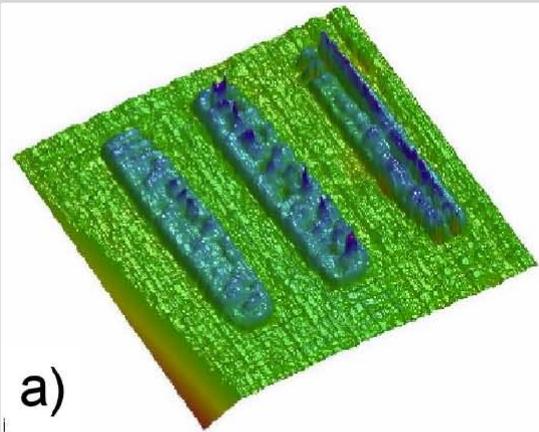
EEa



EEp

DHM.vi demo





C.J. Mann, L.F. Yu, C.M. Lo, and M.K. Kim, "High-resolution quantitative phase-contrast microscopy by digital holography". *Optics Express*, 13: p. 8693-8698 (2005).

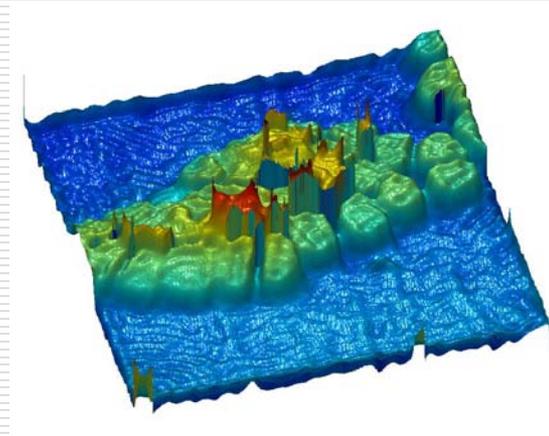
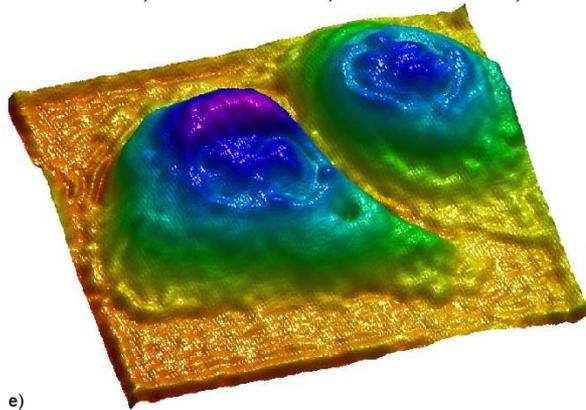
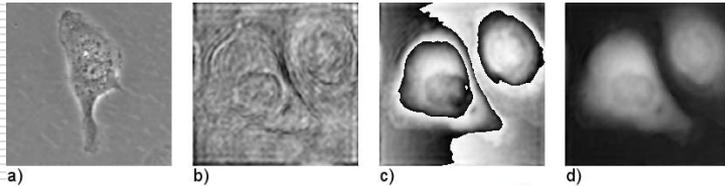
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Unwrapping of 2π -discontinuities in phase images

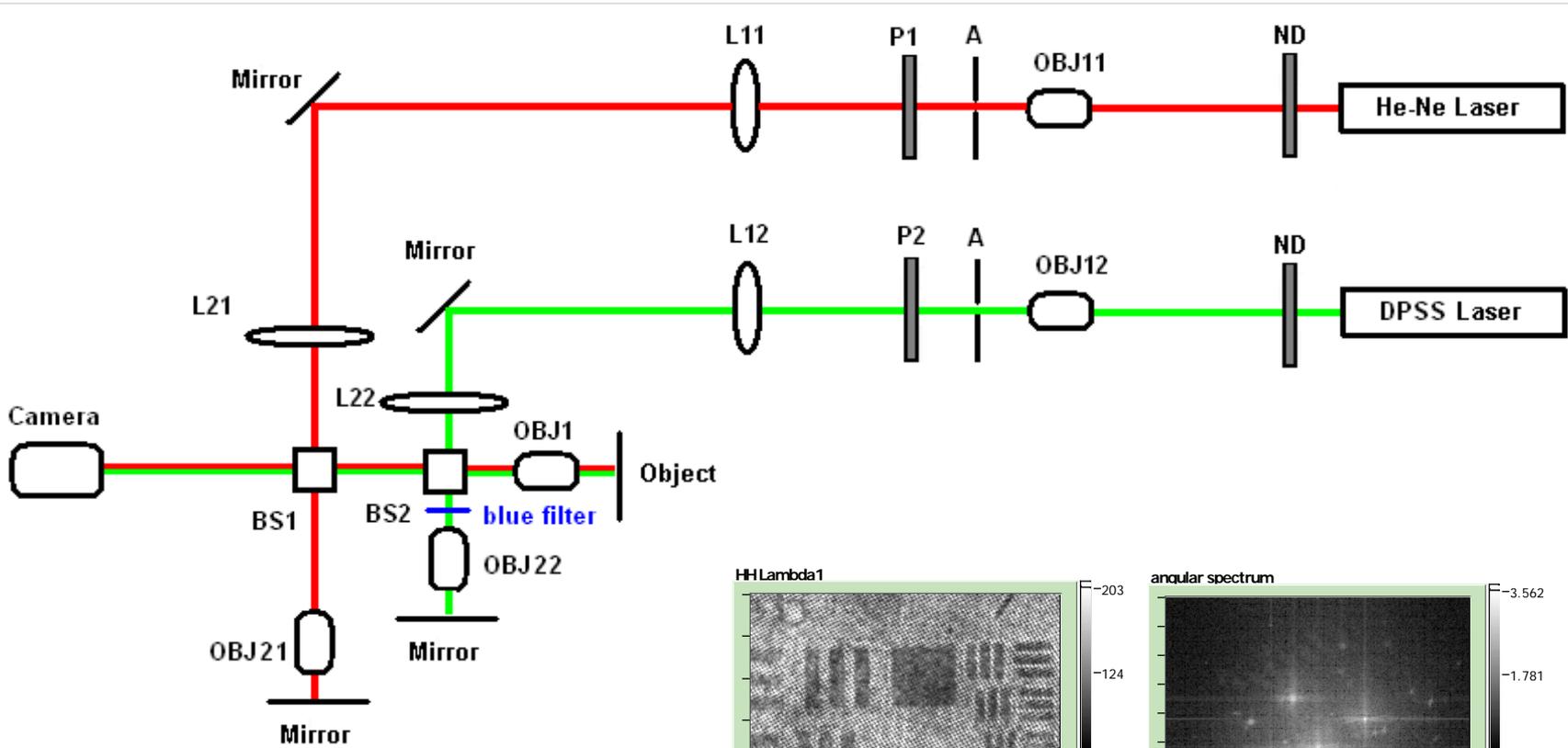
Software-unwrapping

- Detection of discontinuities & addition of integer-multiples of 2π
- Subjective and ambiguous topologies
- Very computation intensive: ~ 5 minutes per image for images presented here

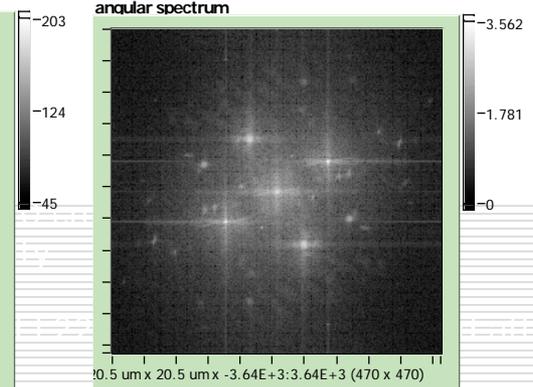
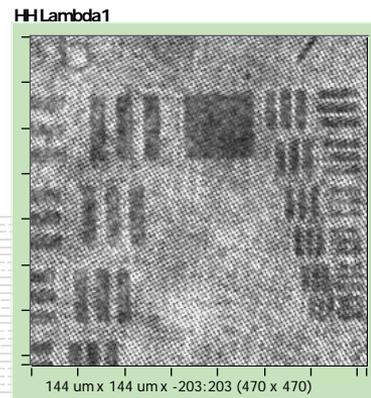


- **Optical phase-unwrapping**
- Two- or three-wavelength interference technique
- Completely deterministic
- Very fast ~ 100 ms
- Light computational load

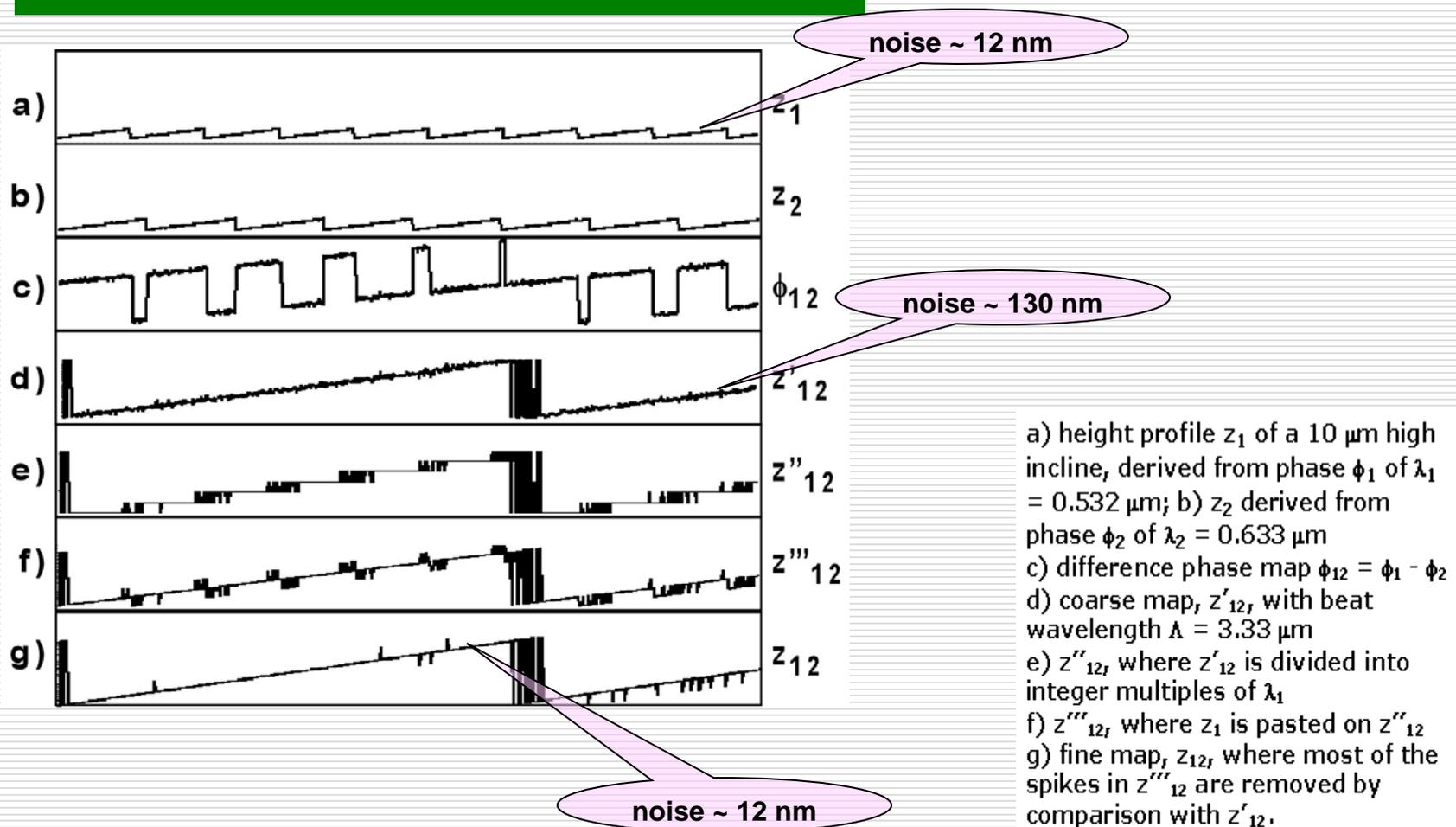
Multi-wavelength Digital Holography Apparatus



Lenses, L1 and L2 has focal length of 175 mm. ND filter, and polarizer, P1 and P2 are of 1/10th wave. Apertures, A is to select only the central part of the beams, are collimated between L11 and L12, L21 and L22. The beam is kept at 100



Dual-wavelength phase imaging digital holography



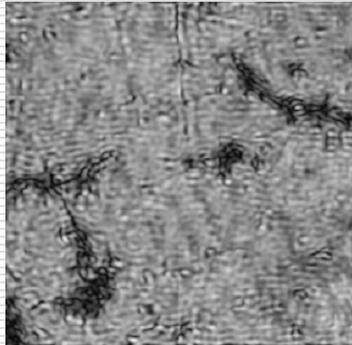
$$\Lambda_{12} = \frac{\lambda_1 \lambda_2}{|\lambda_1 - \lambda_2|} : \text{beat wavelength (Axial range)}$$

a) height profile z_1 of a $10 \mu\text{m}$ high incline, derived from phase ϕ_1 of $\lambda_1 = 0.532 \mu\text{m}$; b) z_2 derived from phase ϕ_2 of $\lambda_2 = 0.633 \mu\text{m}$
 c) difference phase map $\phi_{12} = \phi_1 - \phi_2$
 d) coarse map, z'_{12} , with beat wavelength $\Lambda = 3.33 \mu\text{m}$
 e) z''_{12} , where z'_{12} is divided into integer multiples of λ_1
 f) z'''_{12} , where z_1 is pasted on z''_{12}
 g) fine map, z_{12} , where most of the spikes in z'''_{12} are removed by comparison with z'_{12} .

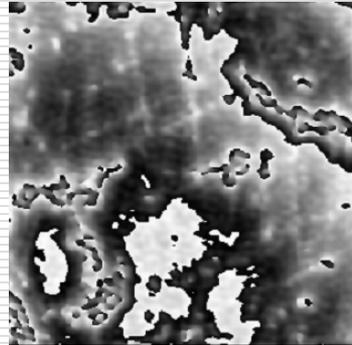
The vertical axis is $5.0 \mu\text{m}$ full scale in every panel, except for c) where the vertical range is -2π to $+2\pi$.

QPM by DH: - OPU vs. software unwrapping

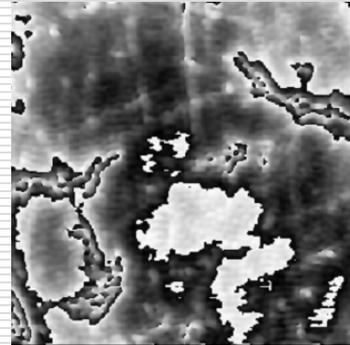
polished coal particle treated with pyrolysis



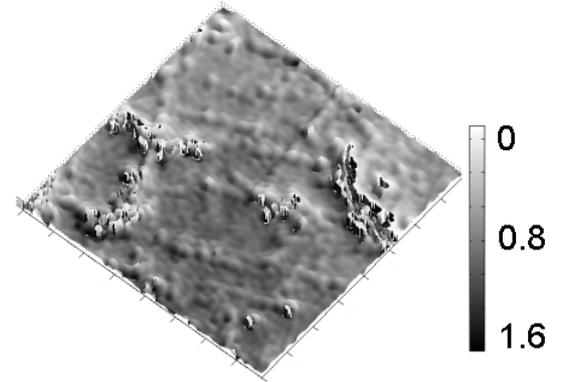
(a)



(b)



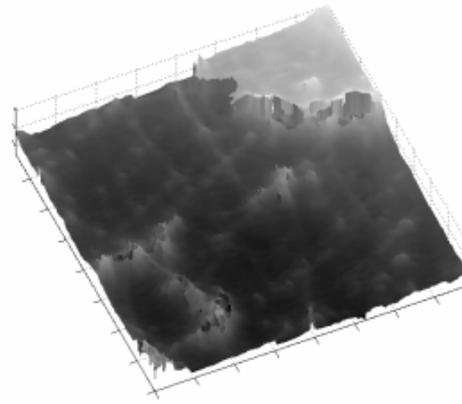
(c)



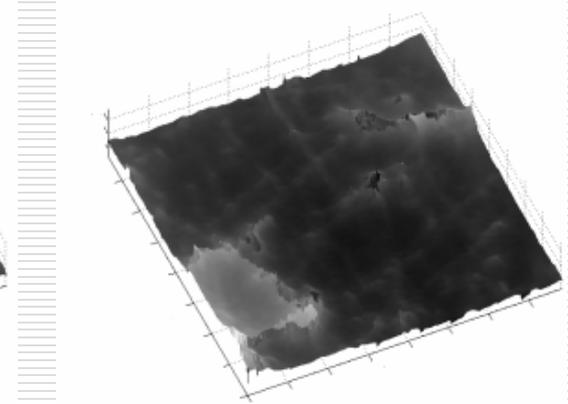
(d)

(a) amplitude image; phase maps reconstructed with (b) 633 nm and (c) 532 nm; (d) 3D rendering of the dual-wavelength phase map (vertical scale in microns);

software unwrapped phase maps reconstructed with (e) 633 nm and (f) 532 nm for comparison. All images are 78x78 microns (256x256 pixels).



(e)



(f)

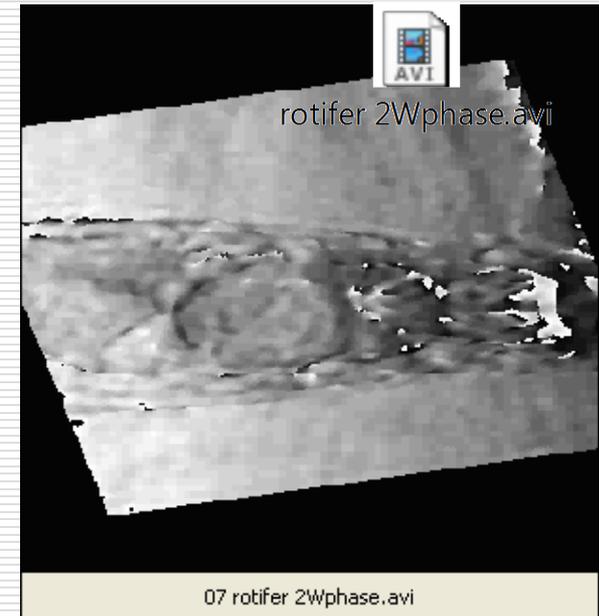
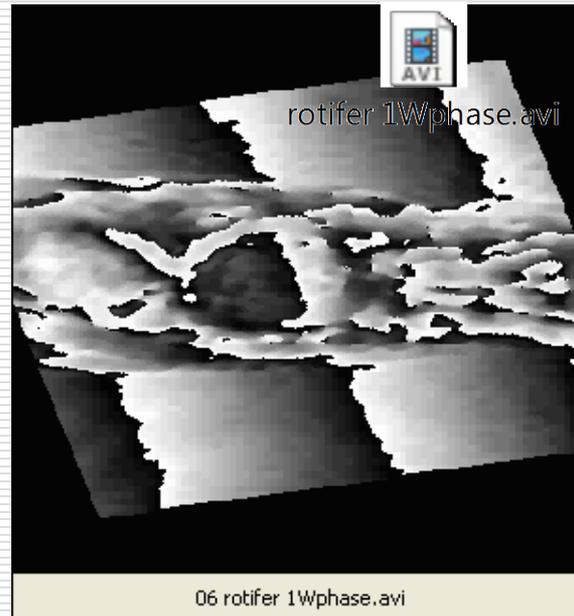
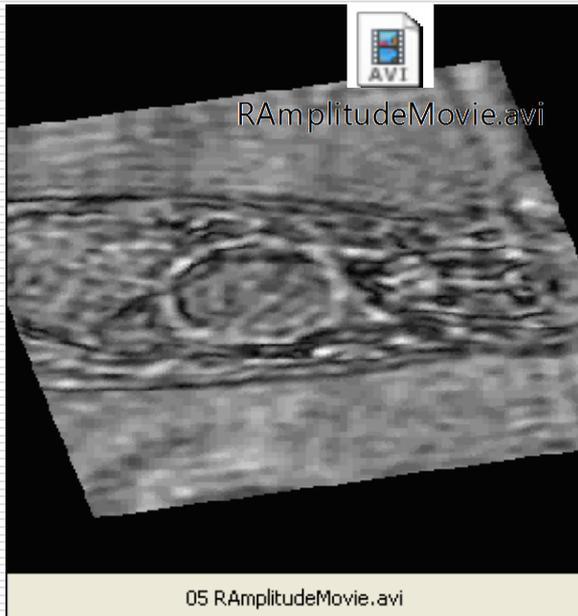
A. Khmaladze, A. Restrepo-Martinez, M. Kim, R. Castaneda, and A. Blandon, "Simultaneous dual-wavelength reflection digital holography applied to the study of the porous coal samples". Applied Optics, 47: p. 3203-3210 (2008).

Dual-wavelength PIDH: movie of live rotifer

amplitude

1W PIDH

2W PIDH



area = $70\mu\text{m} \times 70\mu\text{m}$
pixels = 360×360
 $z = 79\sim 80\mu\text{m}$

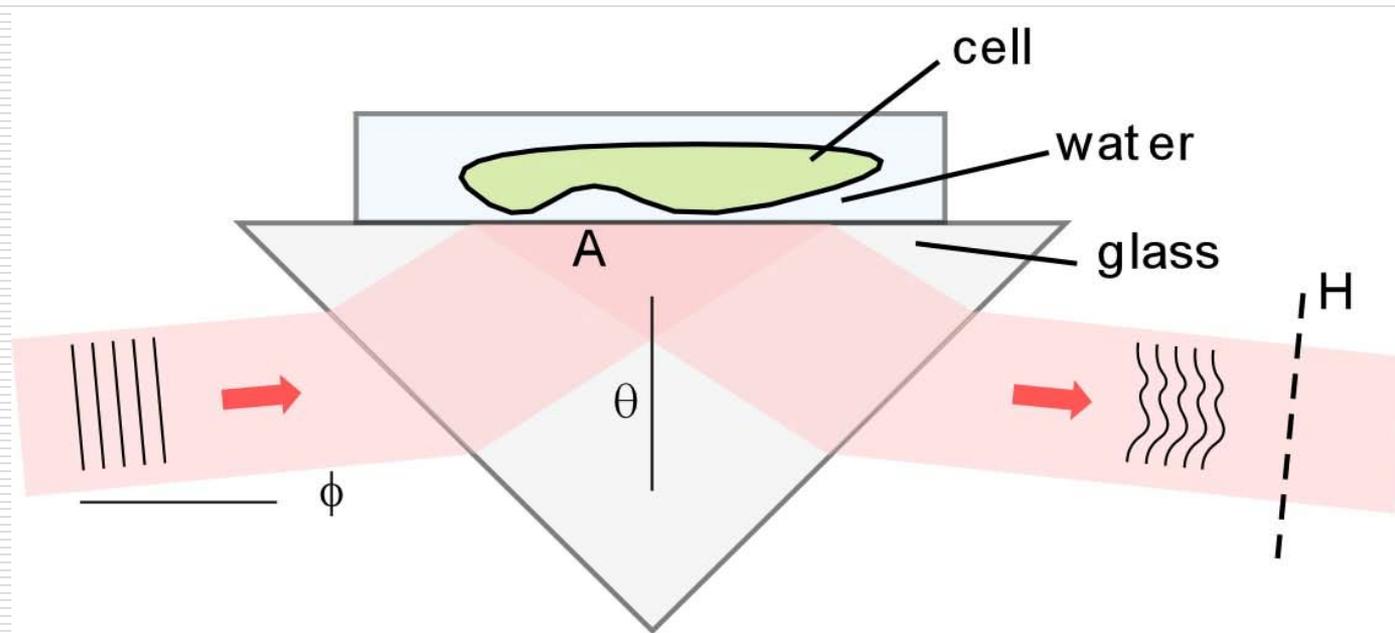
C.J. Mann, L.F. Yu, and M.K. Kim, "Movies of cellular and sub-cellular motion by digital holographic microscopy". Biomed. Eng. Online, 5 (2006).

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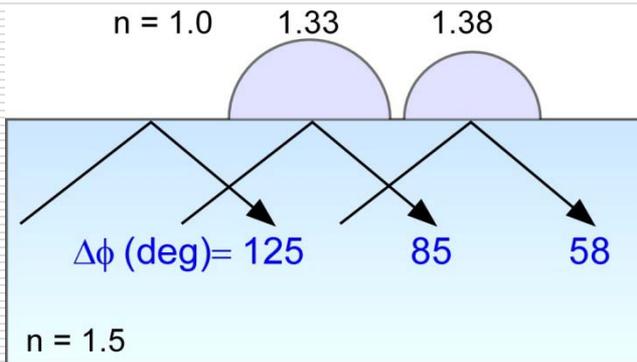
TIRHM: total internal reflection holographic microscopy

- modulation of TIR wavefront by variation of interface
- detection and imaging of modulated wavefront by DH
- quantitative profiling of interface

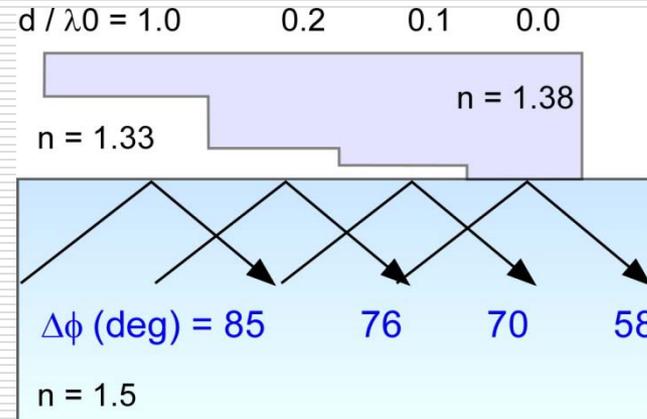


W. M. Ash, and M. K. Kim, "Digital holography of total internal reflection," *Optics Express* 16, 9811-9820 (2008).

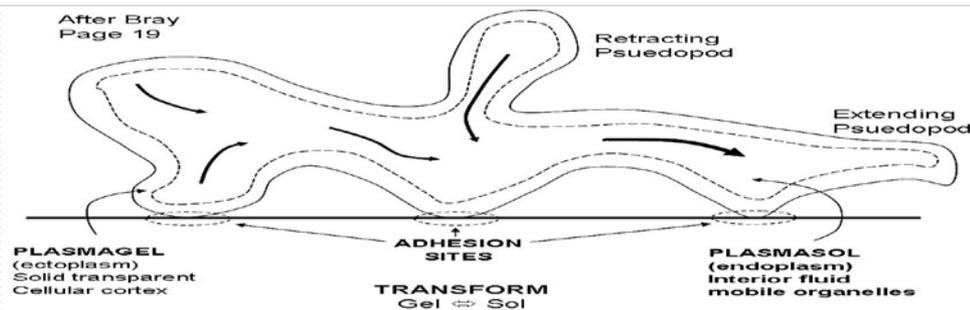
TIRHM imaging modes



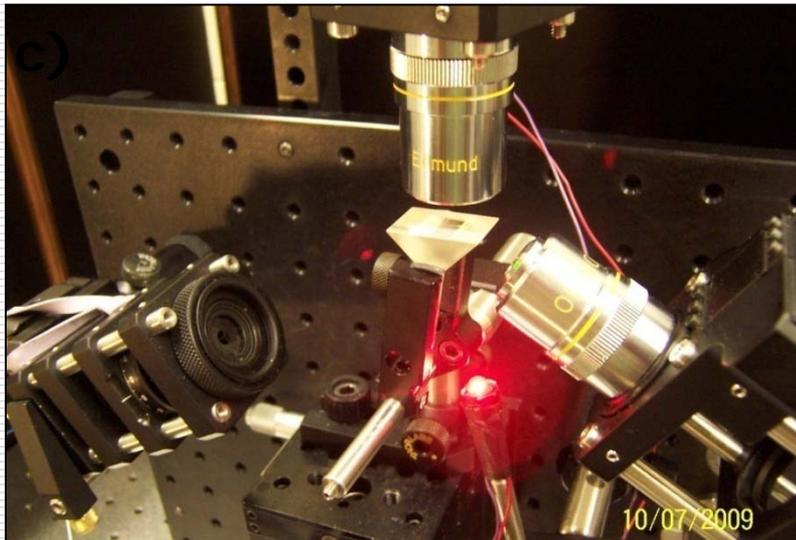
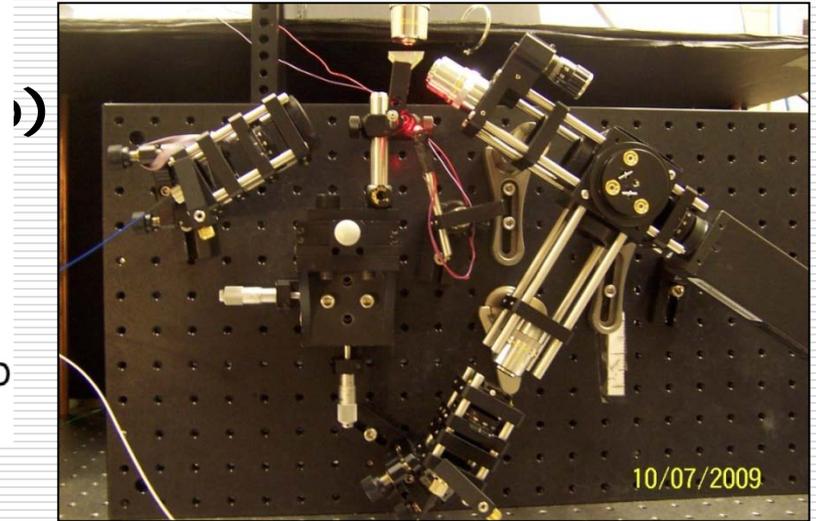
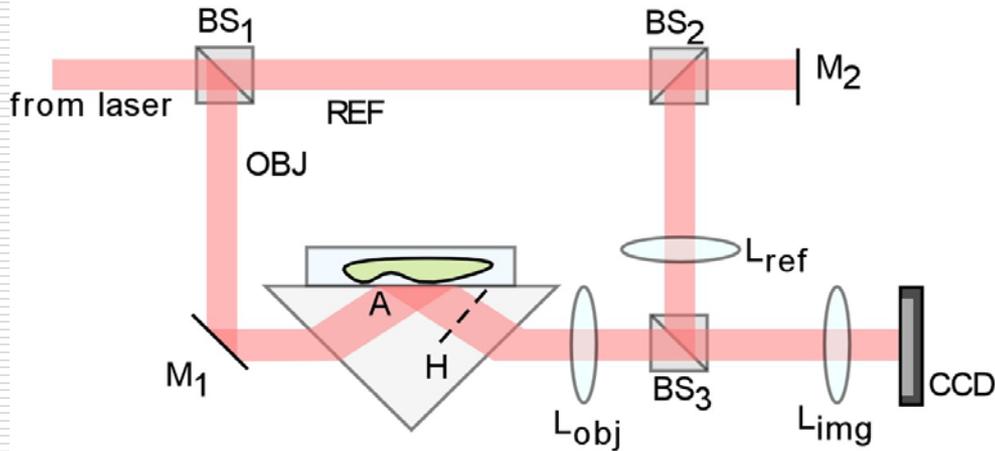
index profile



thickness profile

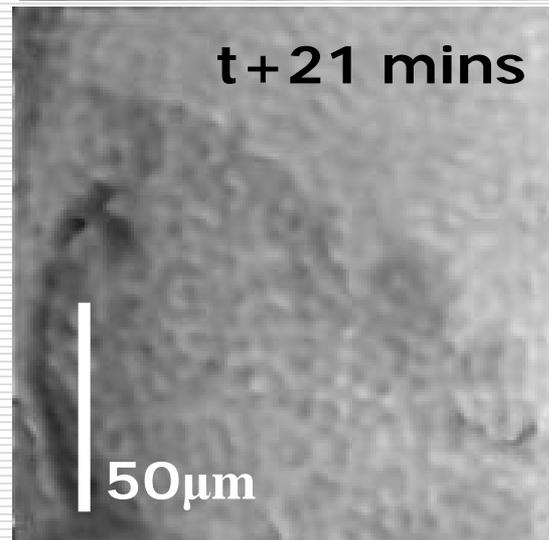
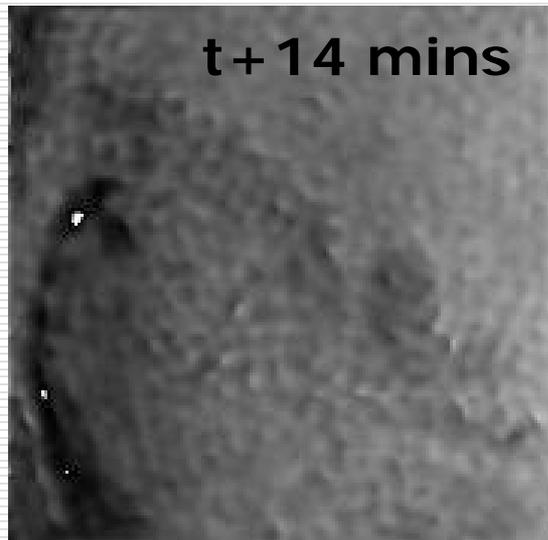
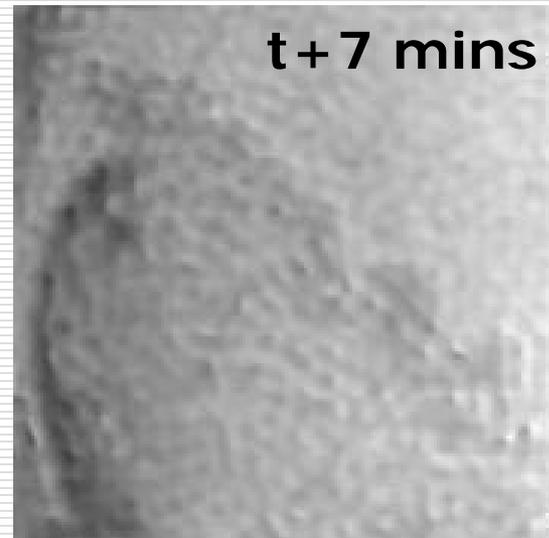
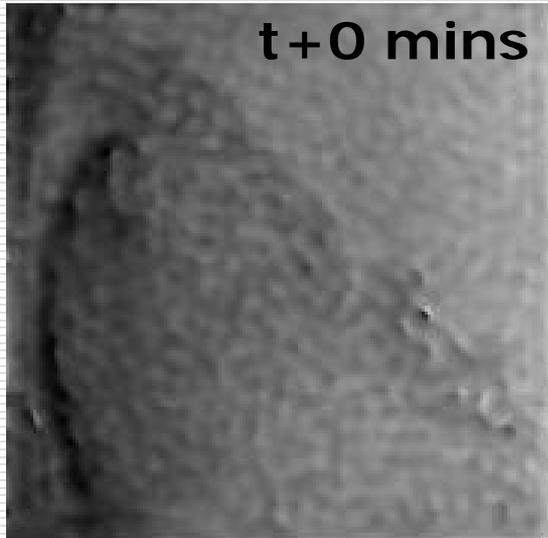


TIRHM Apparatus



- a) Schematic
- Laser- DPSS Nd:YAG @ 532nm
 - Camera- Sony Firewire CCD
- b) Operational system
- c) Close-up of TIR prism
- w/ 10x microscope objectives

Amoeba Sample: Time lapse phase imagery



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laser cellular microsurgery apparatus

- Nd:YVO4 laser for microsurgery: 0.4uJ/pls, 12ns, 20kHz, 10e9W/cm2
- LD for holographic microscopy

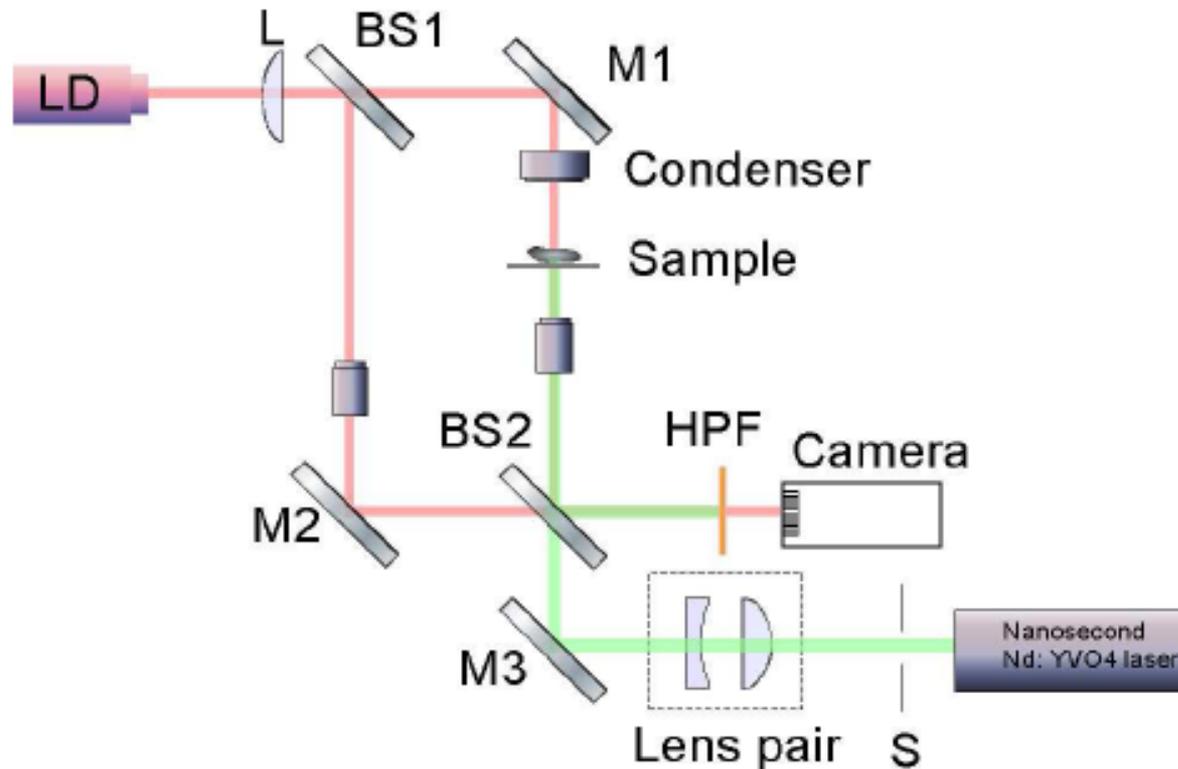
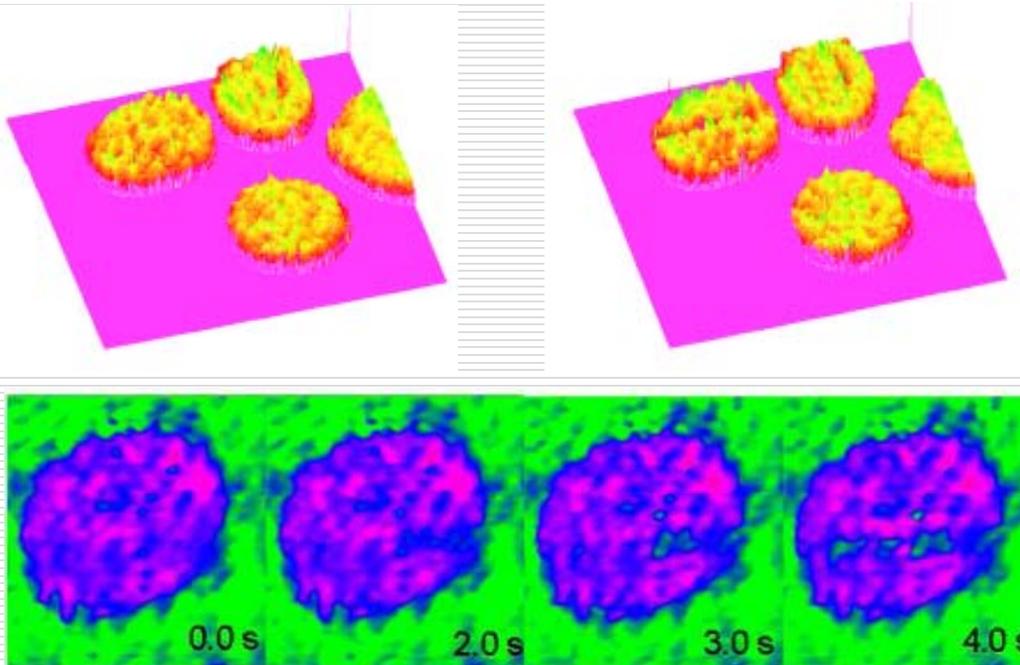


Fig. 1. Schematic of the experimental setup. LD is the 675nm laser diode; BS1 and BS2 are beam splitters; Ms are mirrors; S is a shutter; L is a lens; HPF is a high-pass filter for red light.

quantitative phase microscopy of cellular laser microsurgery

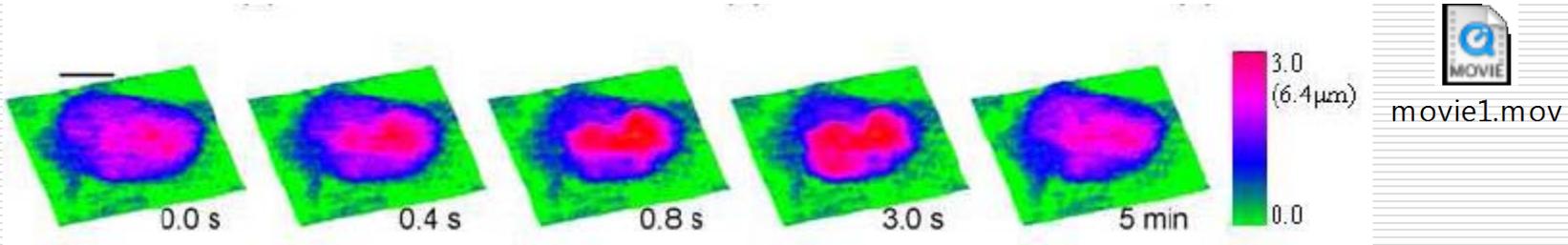
- laser microbeam
 - study cell structure and function
 - injection of exogenous materials
 - free the internal constituents
 - study developing organisms—such as in the formation of the nervous system
 - reduce the thickness of the zona pellucida layer of the ovum to improve human in vitro fertility

- quantitative phase evaluation by DHM during laser incision of red blood cells

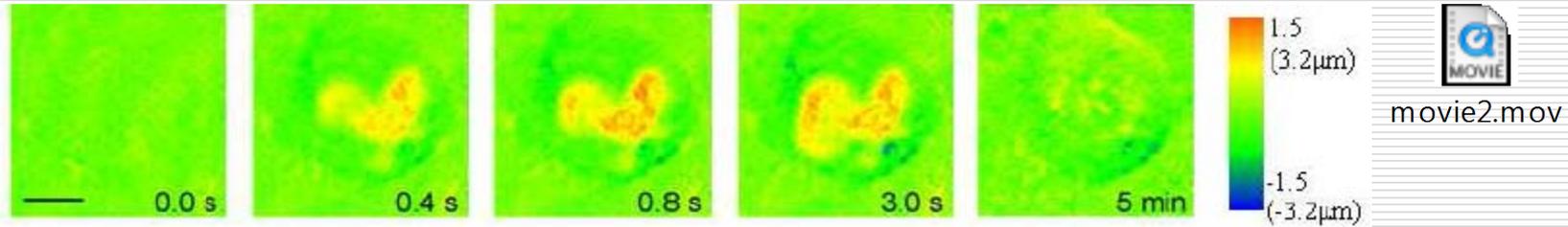


DHM movies of laser microsurgery

- rat kangaroo kidney epithelial (PTK2) cells:

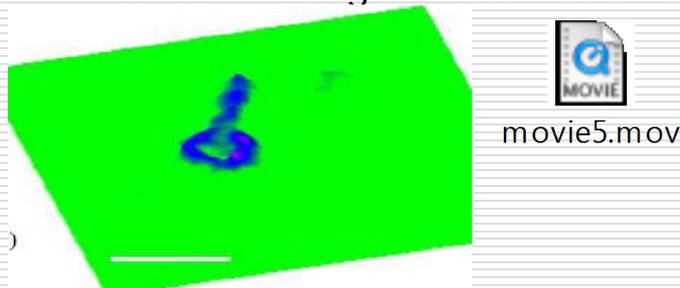


phase image movie during surgery



phase change movie : swelling of chromosomes during ablation, with subsequent recovery after laser is removed.

- rod cell from goldfish retina: drastic morphological change following a slight damage of one end of cell

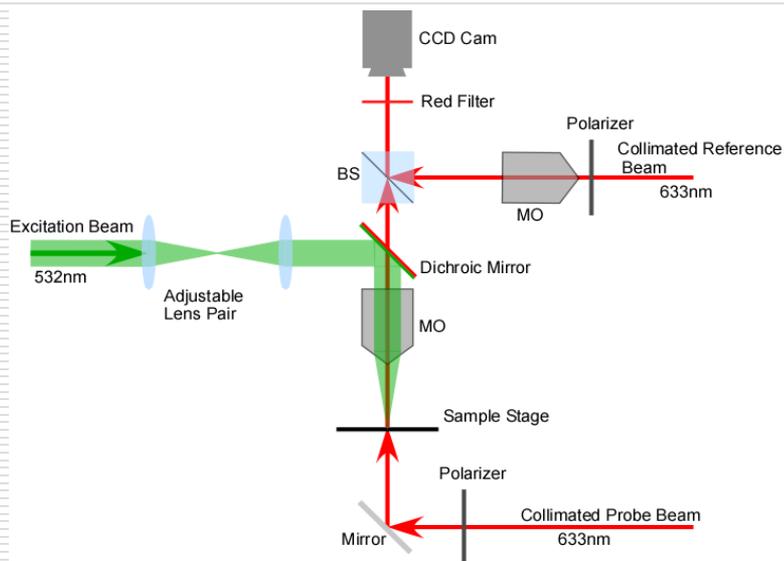


L Yu, S Mohanty, J Zhang, S Genc, MK Kim, MW Berns, Z Chen, "Digital holographic microscopy for quantitative cell dynamic evaluation during laser microsurgery," Opt. Express 17, 12031-12038 (2009)

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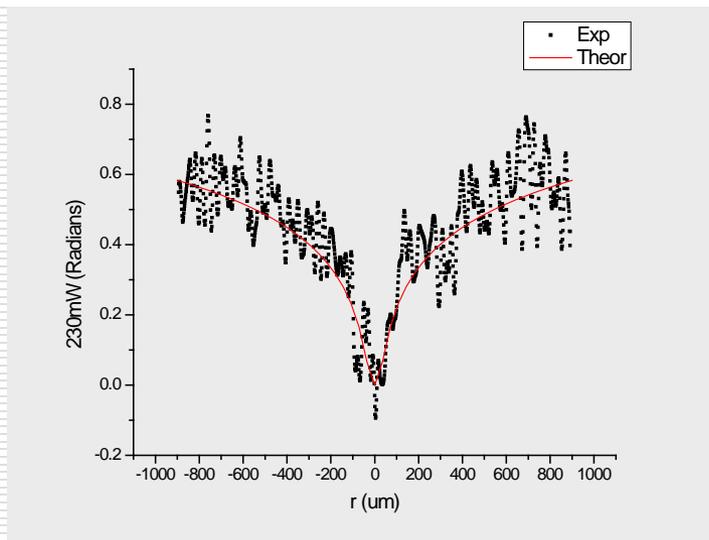
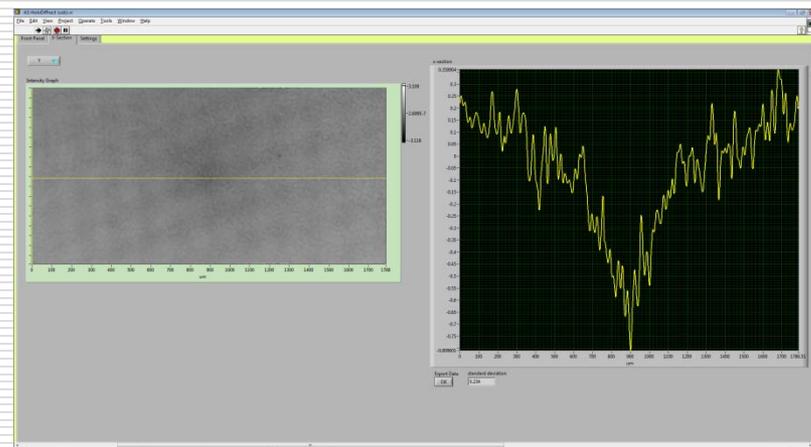
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Thermal Lensing and Absorption Coefficient



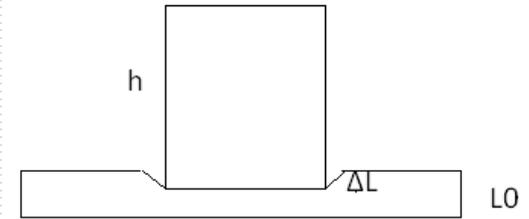
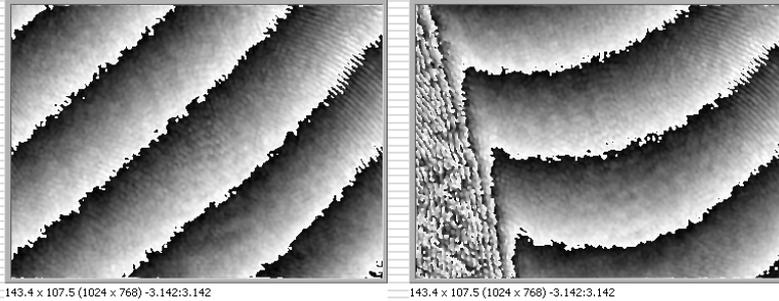
$$\phi = \theta \int_0^t \frac{1}{1 + 2t'/\tau} \left[1 - \exp\left(-\frac{2r^2/w^2}{1 + 2t'/\tau}\right) \right] \frac{dt'}{\tau}$$

$$\theta = -\frac{P\alpha l (dn/dT)}{\kappa\lambda}$$

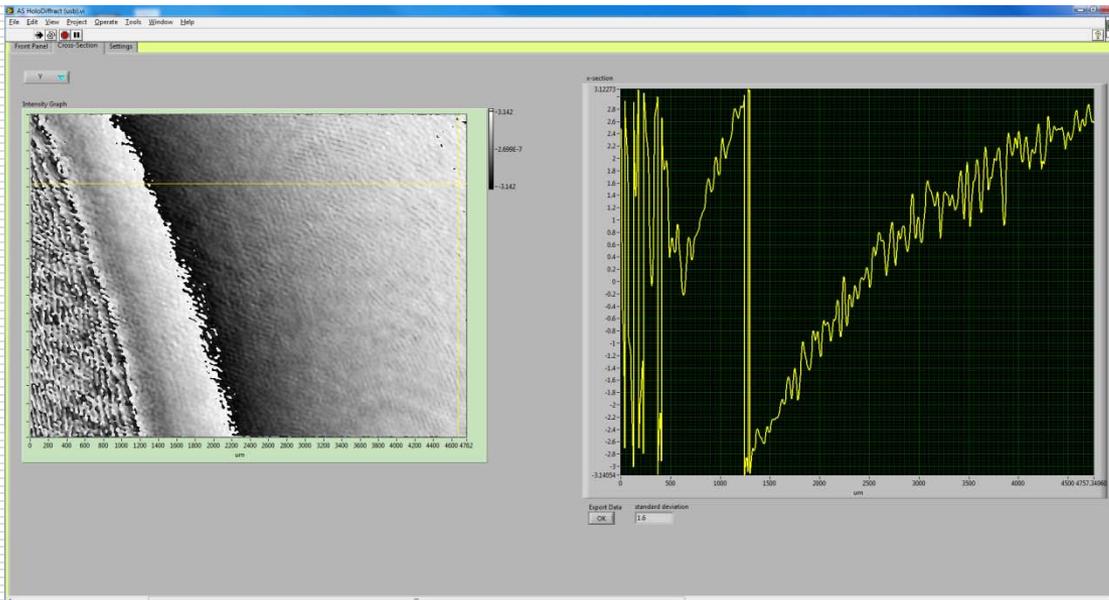


Absorption coefficients of 4.5×10^{-4} and $3.8 \times 10^{-4} \text{ cm}^{-1}$ (@532nm) were successfully determined for our samples of methanol and ethanol,

Deformation and Young's Modulus Measurement of Thin Film



2 mm dia x 0.5 mm height
brass plate (13.5 mg) on 1
mm thick polyacrylamide
film



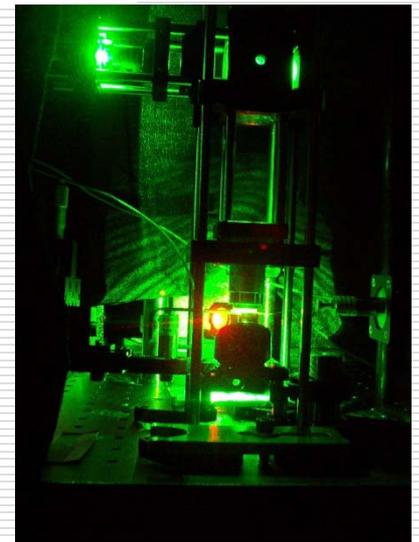
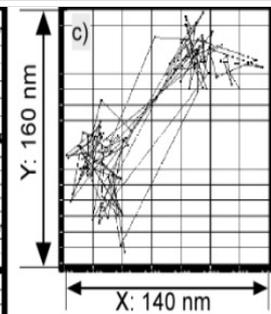
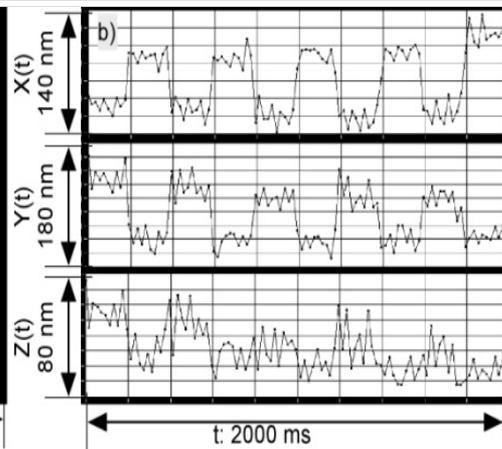
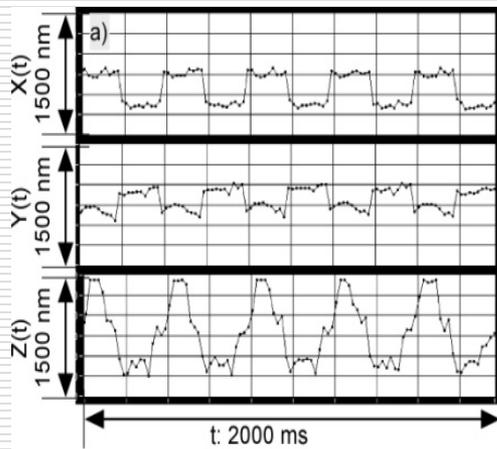
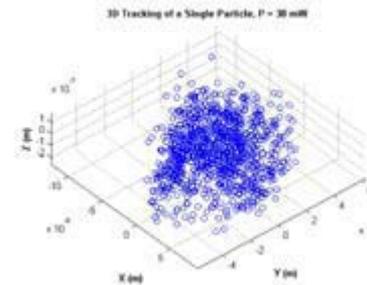
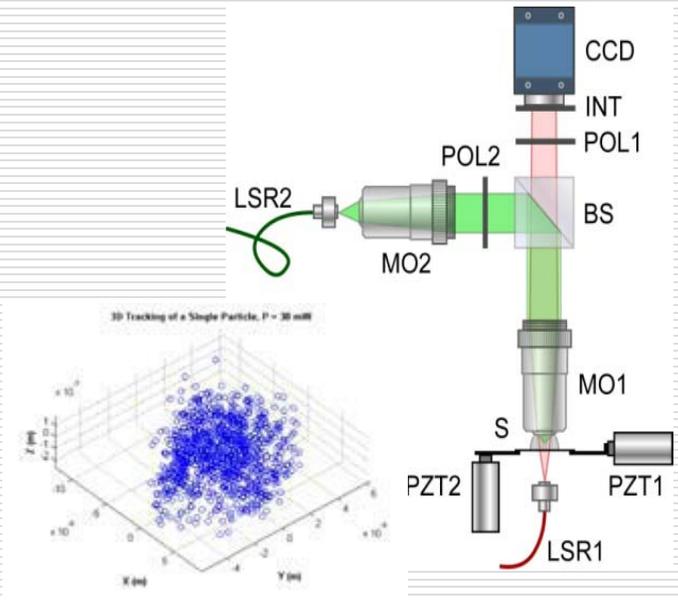
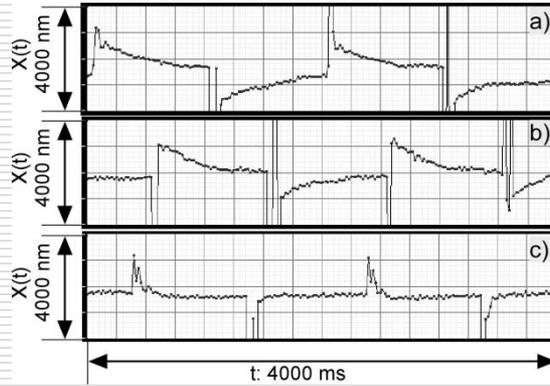
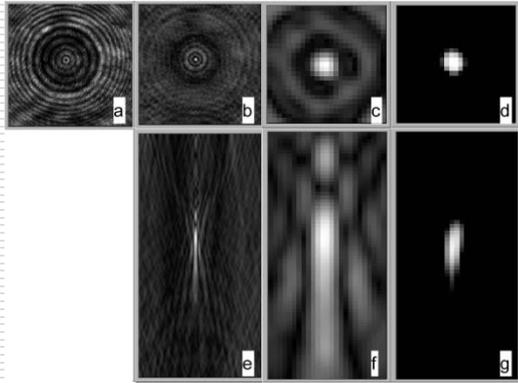
Young's modulus of polyacrylamide film
measured to be 14.5 kN/m²

Applications:

- Force measurement of cellular motility
- Characterization of polyelectrolyte multilayer film growth for tissue engineering

Digital Gabor holography for particle tracking

- polystyrene (10 μ m) spheres fixed on cover slip
- piezo transducer drives for x- and z-movements
- sub-nanometer control of x,z-movements



Adaptive Optics without wavefront sensor or corrector

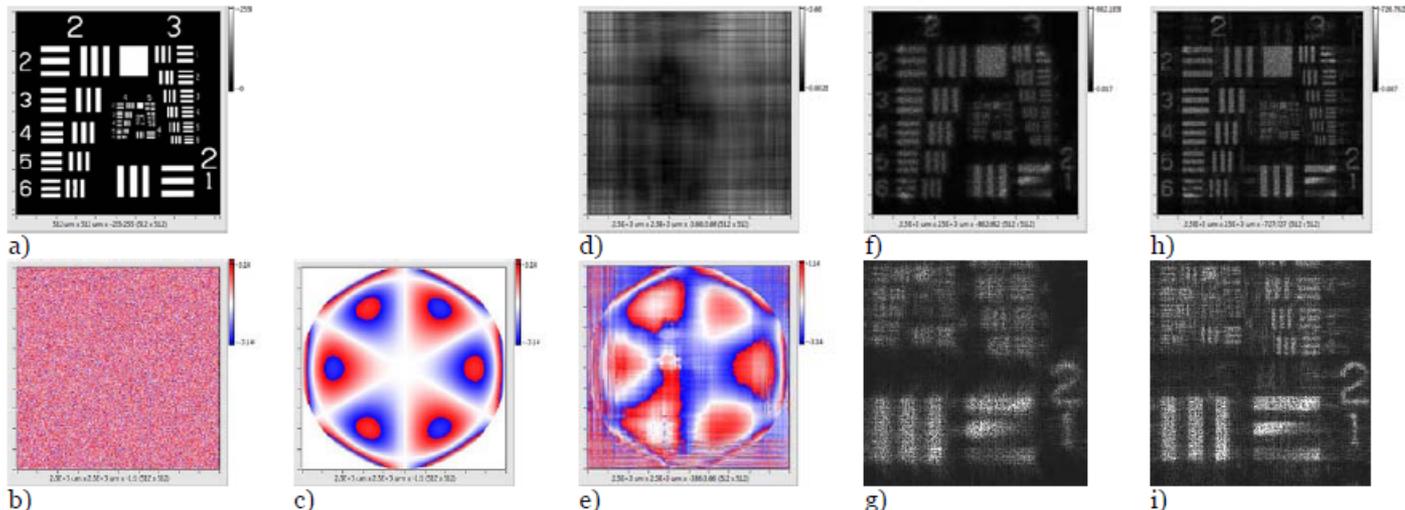
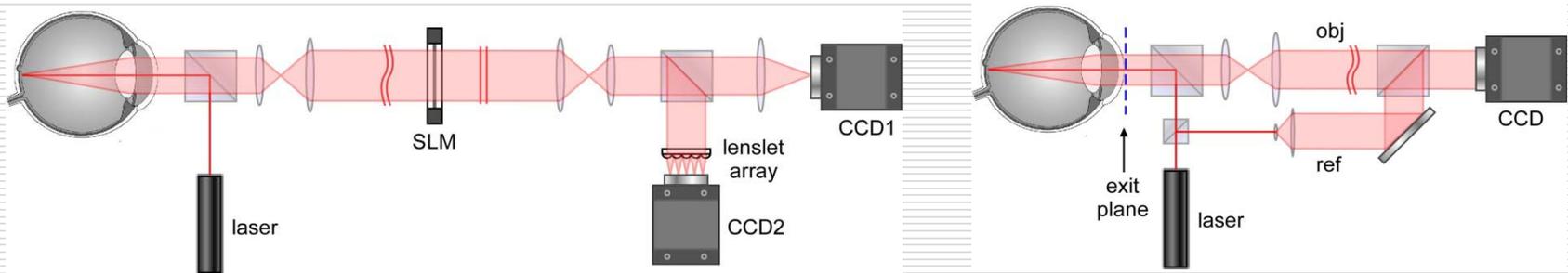
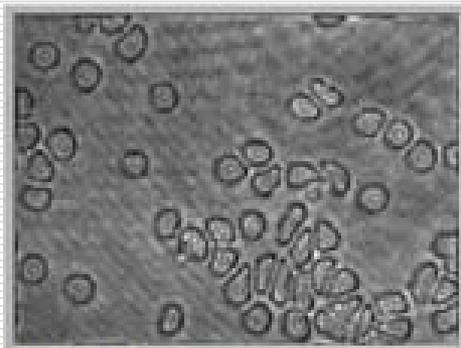


Fig. 2: Simulation of DHAO process. Amplitude image are shown in gray scale and phase images (b,c, & e) in blue-white-red color scale, representing the range of phase from $-\pi$ to $+\pi$. a) Assumed amplitude pattern on retina; b) phase noise of retinal surface; c) assumed aberration of the eye; d) amplitude of exit field; e) phase of exit field, representing recovered aberration of the eye; f) uncorrected image of retina and g) its detail; and h) corrected image of retina and i) its detail.

Multi-mode contrast generation from a single hologram

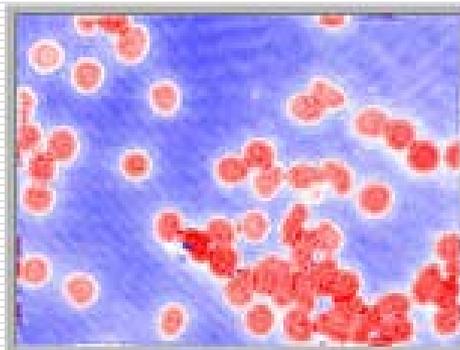
- Multi-mode contrast generation from a single hologram: a) amplitude contrast; b) quantitative phase contrast; c) dark field; d) Zernike phase contrast; e) DIC; f) spiral DIC.

amplitude contrast



146 x 109.5 (1024 x 768) 0.0001089:0.2807

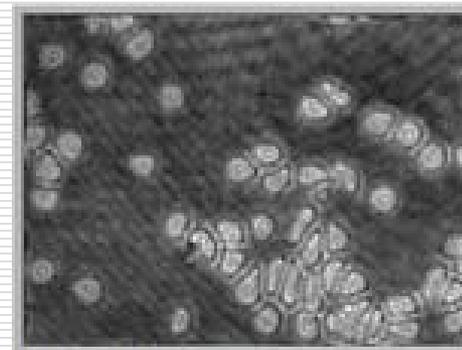
amplitude contrast



146 x 109.5 (1024 x 768) -3.141:3.142

Dark field

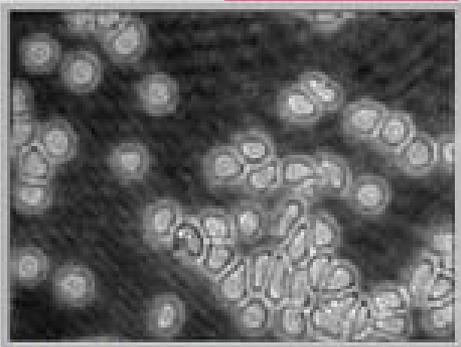
$$1 - \delta(f_x, f_y)$$



146 x 109.5 (1024 x 768) 0.0006224:0.2971

ZPC

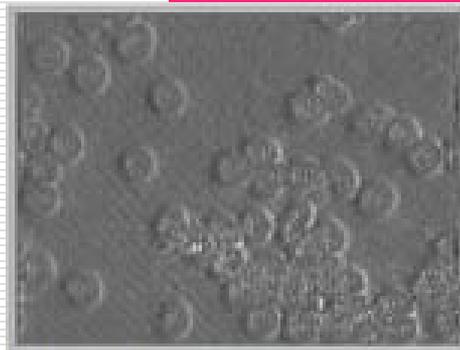
$$1 - (1 - i)\delta(f_x, f_y)$$



146 x 109.5 (1024 x 768) 0.000248:0.318

DIC

$$\exp[2\pi i(f_x \Delta_x + f_y \Delta_y)]$$



146 x 109.5 (1024 x 768) -0.0006667:0.001049

spiral DIC

$$\exp(i\theta)$$



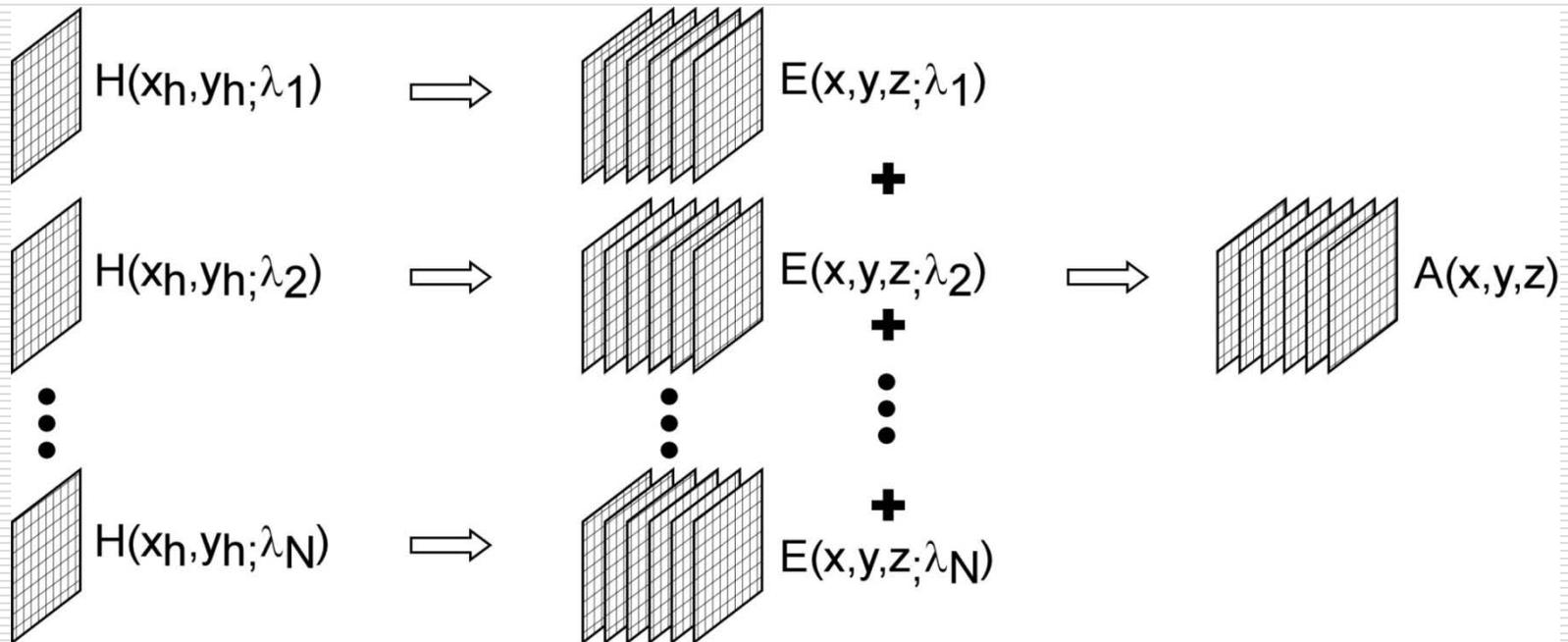
152.1 x 114.1 (1024 x 768) 0.0001939:0.3405

outline

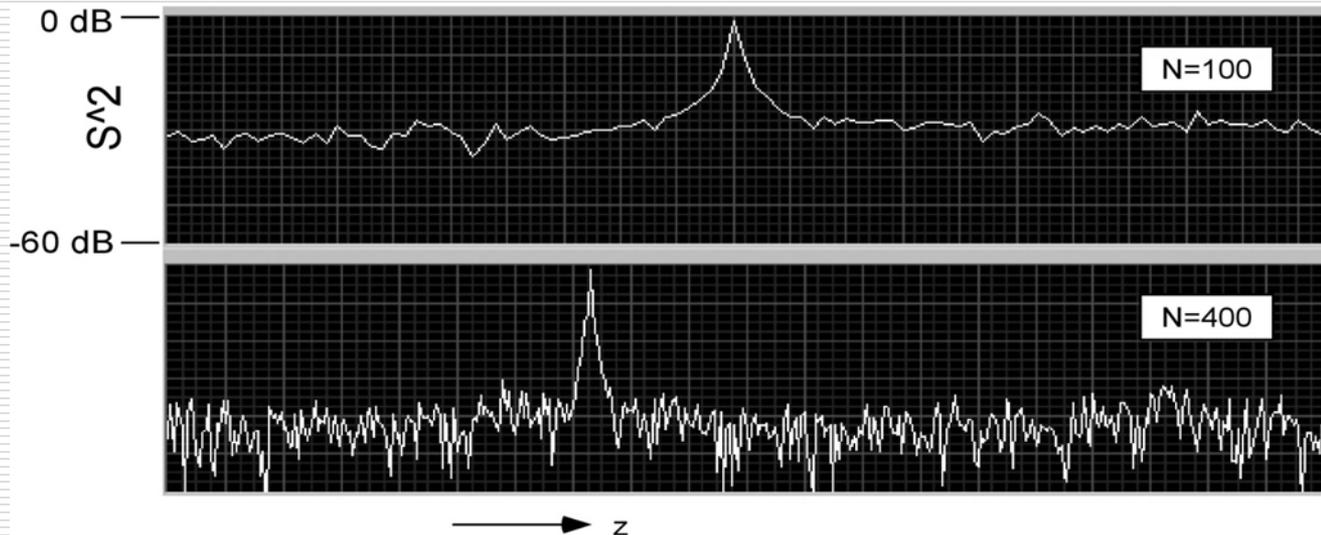
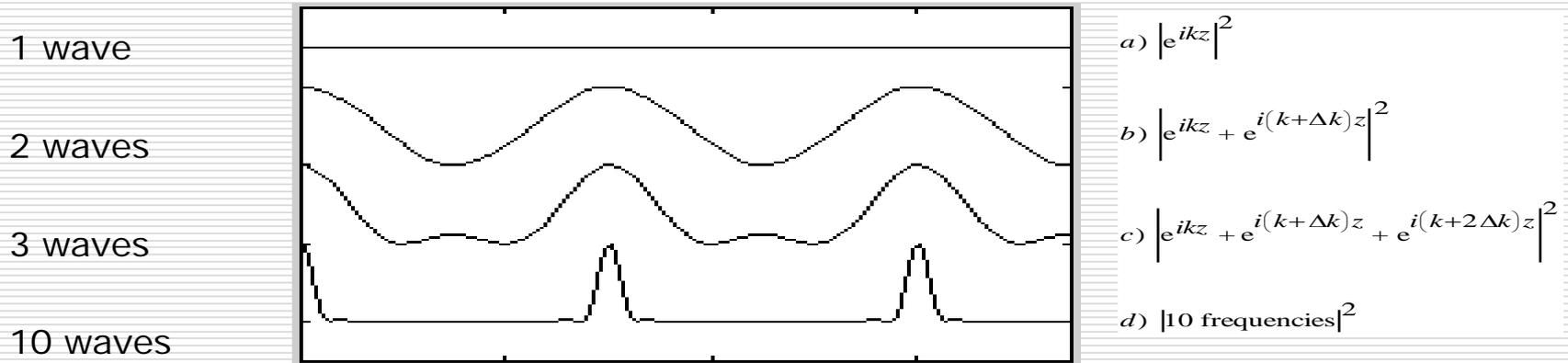
- DHM: Digital Holographic Microscopy
- OPU: Optical Phase Unwrapping
- TIRHM: Total Internal Reflection Holographic Microscopy
- DHM of Laser Microsurgery
- Some current projects
- **Optical Tomography and Topography**
- Conclusions

Digital Interference Holography: the process

- acquire a hologram from camera
- calculate 2D optical field array at many equally spaced z-distances
 - this produces 3D volume of optical field for one wavelength
- step the wavelength
 - and calculate another 3D volume of optical field for the new wavelength
- calculate 3D volumes of optical field for many wavelengths
- numerically superpose all 3D volumes of optical field
- final single volume of optical field with tomographic peaks

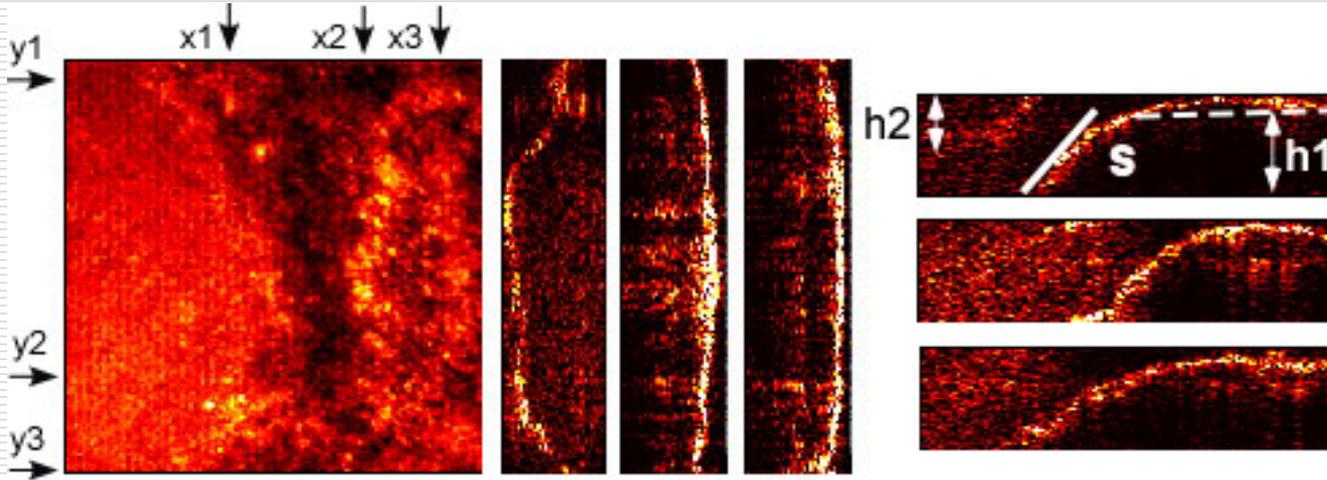
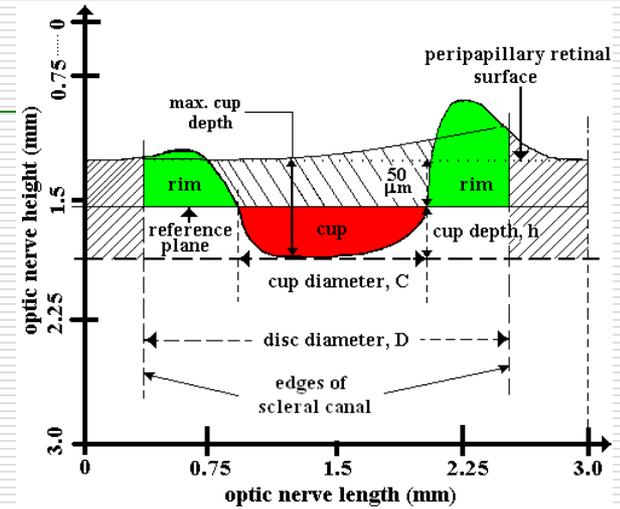
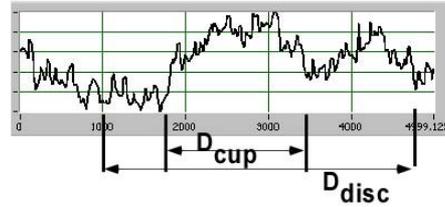
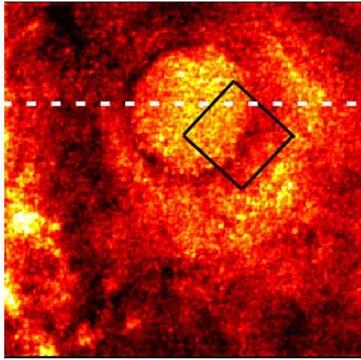


superposition of many wavelengths



- axial range: $\Lambda = \lambda^2/\Delta\lambda$
- axial resolution: $\delta = \Lambda/N$

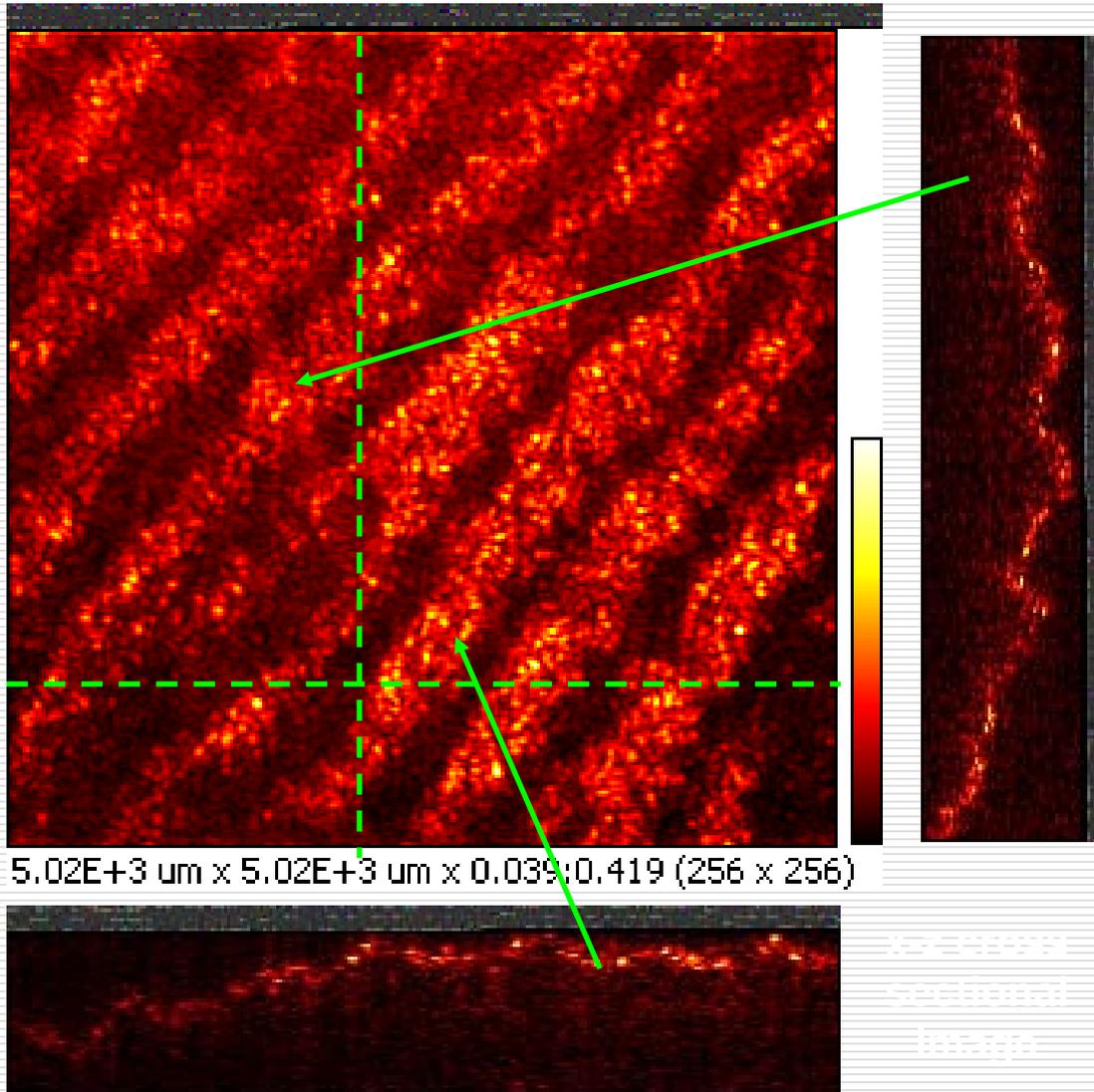
3D human optic nerve disk



(a) x-y cross-section, FOV=1100 x 1100 μm^2 ; (b) y-z cross sections at various x values, 1100 x 280.35 μm^2 , from left to right, x1, x2, and x3; (c) x-z cross sections at various y values, 280.35 x 1100 μm^2 , from top to bottom, y1, y2, and y3; Z = 29.7 μm ; NX= NY=256 pixels; NZ= 50 pixels; s = the slope; h1, h2: heights.

M.C. Potcoava, C.N. Kay, M.K. Kim, and D.W. Richards, "In vitro imaging of ophthalmic tissue by digital interference holography". Journal of Modern Optics, 57: p. 115-123 (2010).

3D fingerprints by DIH



$5.02E+3 \text{ } \mu\text{m} \times 5.02E+3 \text{ } \mu\text{m} \times 0.039:0.419 \text{ (} 256 \times 256 \text{)}$

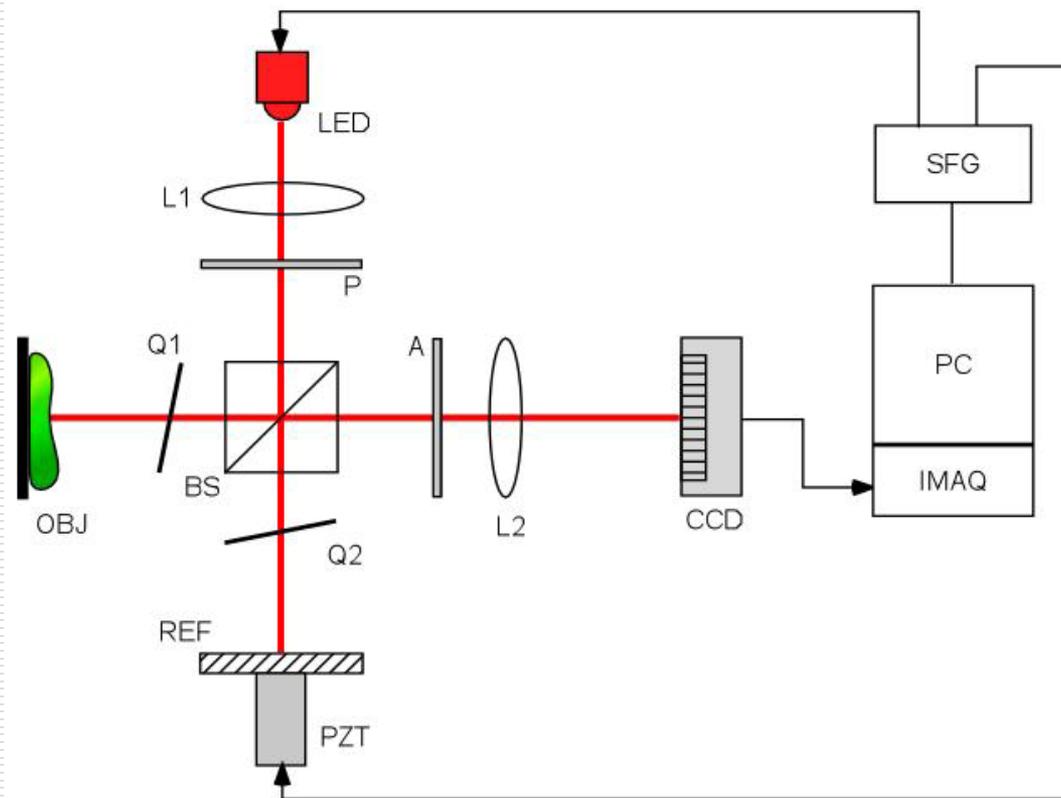
FOV = 5 x 5 mm
 $\Delta\lambda$: 0.560-0.600 μm
Z = 742.57 μm
 Λ = 420.5 μm
dz = 8.41 μm
DX = DY = 19.6 μm
NX x NY x NZ =
256 x 256 x 50

y-z cross
sectional
image

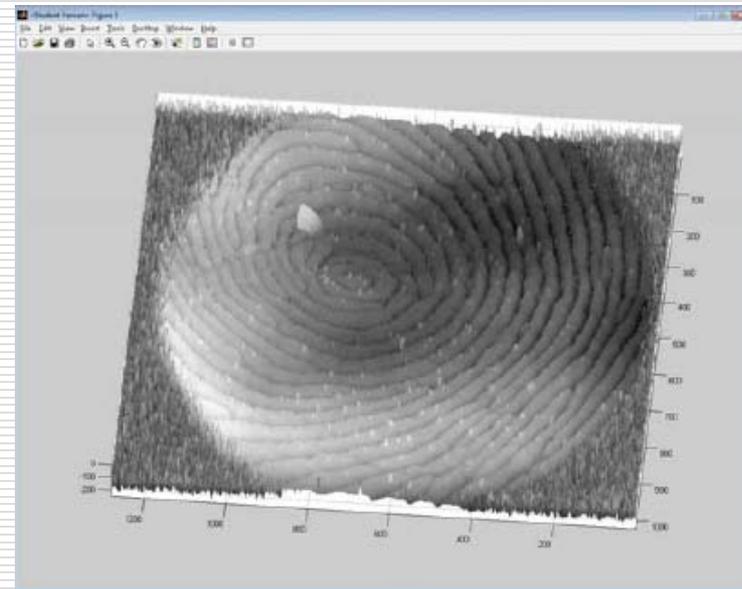
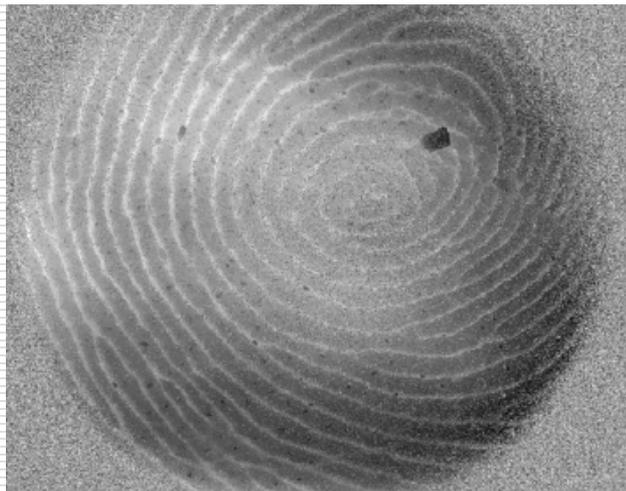
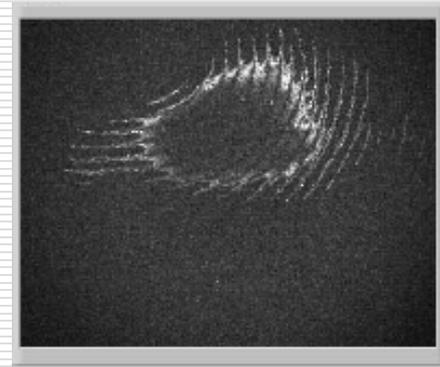
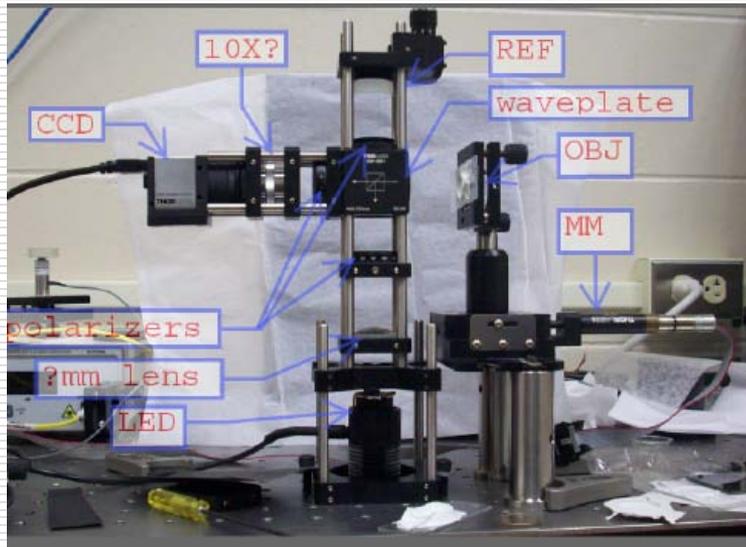
x-z cross
sectional
image

full-color wide-field OCT by PSIM

OCT: optical coherence tomography



3D fingerprint by PSIM



MC Potcoava & MK Kim, "Fingerprint biometry applications of digital holography and low-coherence interferography," Appl. Opt. 48, H9-15 (2009)

color WFOCT: colored dime



X-Y



X-Z



3D

image volume = 7.2mm x 7.2mm x 335um

voxels = 480 x 480 x 67

voxel volume = 15um x 15um x 5um

L.F. Yu and M.K. Kim, "Full-color three-dimensional microscopy by wide-field optical coherence tomography". Optics Express, **12**: p. 6632-6641 (2004).

Conclusions: Capabilities of DHM

- High resolution quantitative phase microscopy
- Single-exposure image capture and numerical focusing
- Versatile manipulation of complex optical fields
 - Numerical focusing
 - Aberration,
 - Wave front curvature, etc.

- Quantitative label-free microscopy of live cellular and intra-cellular structures and processes
- Biomedical tissue tomography: ophthalmology
- Microstructure imaging and testing
- Particle imaging and tracking: cytometry
- Biomaterials characterization
- etc. ...

Thank You!